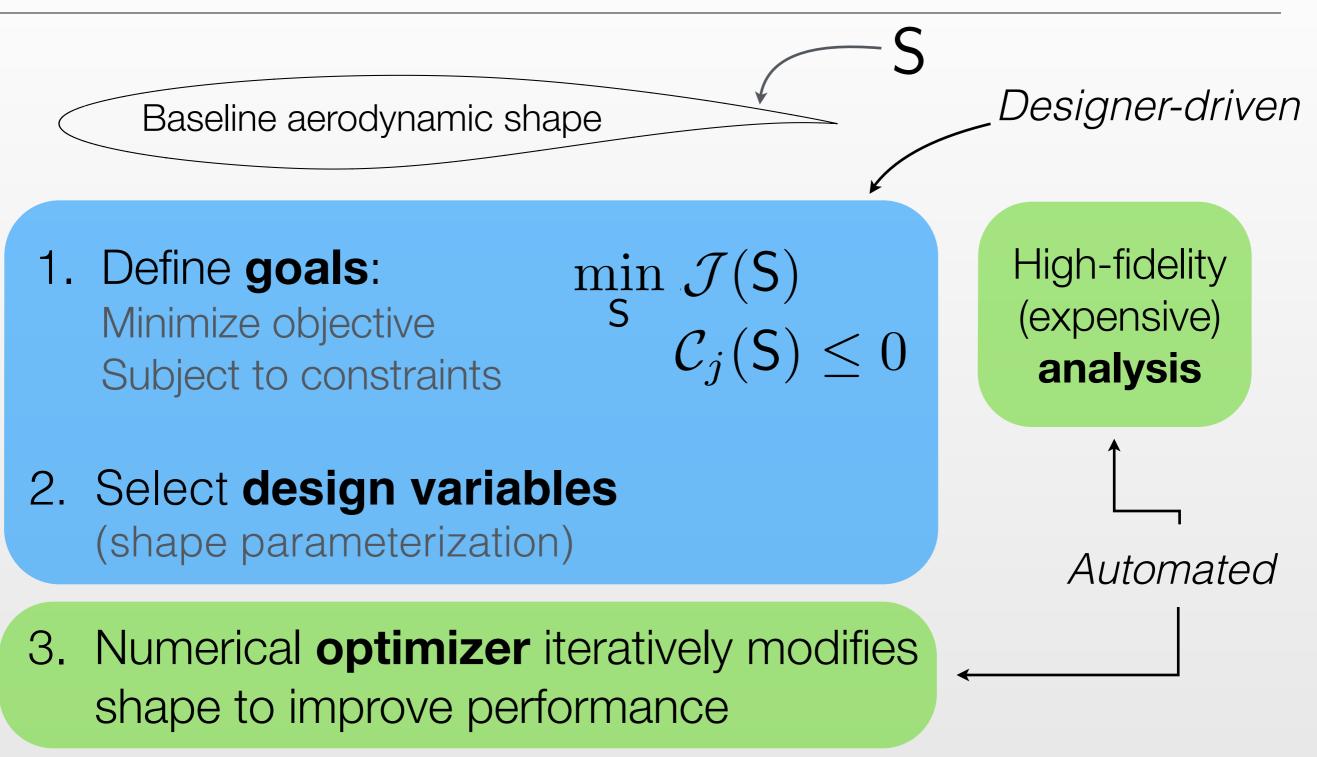




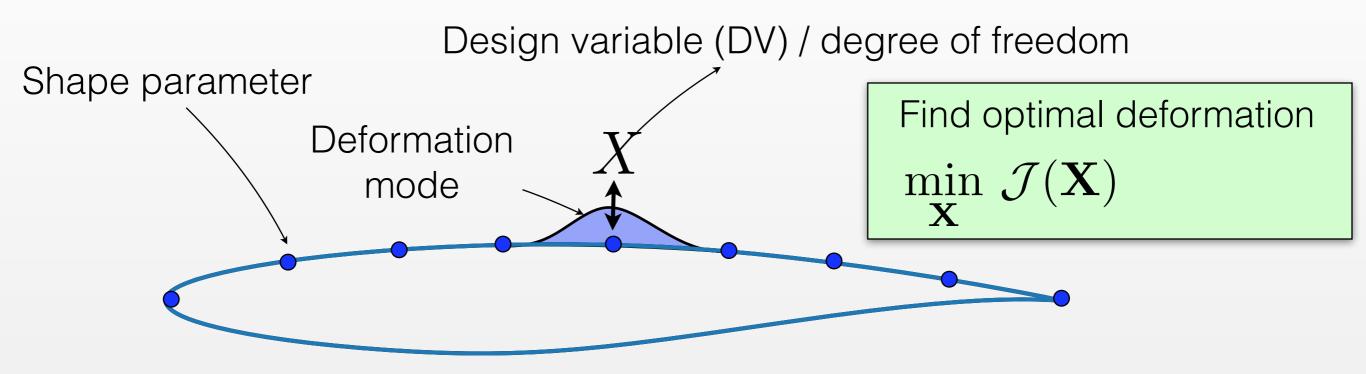
- 1. Introduction to Shape Parameterization
- 2. Automatic Adaptive Parameterization
- 3. Verification Studies
- 4. Design Examples

# Aerodynamic Shape Optimization



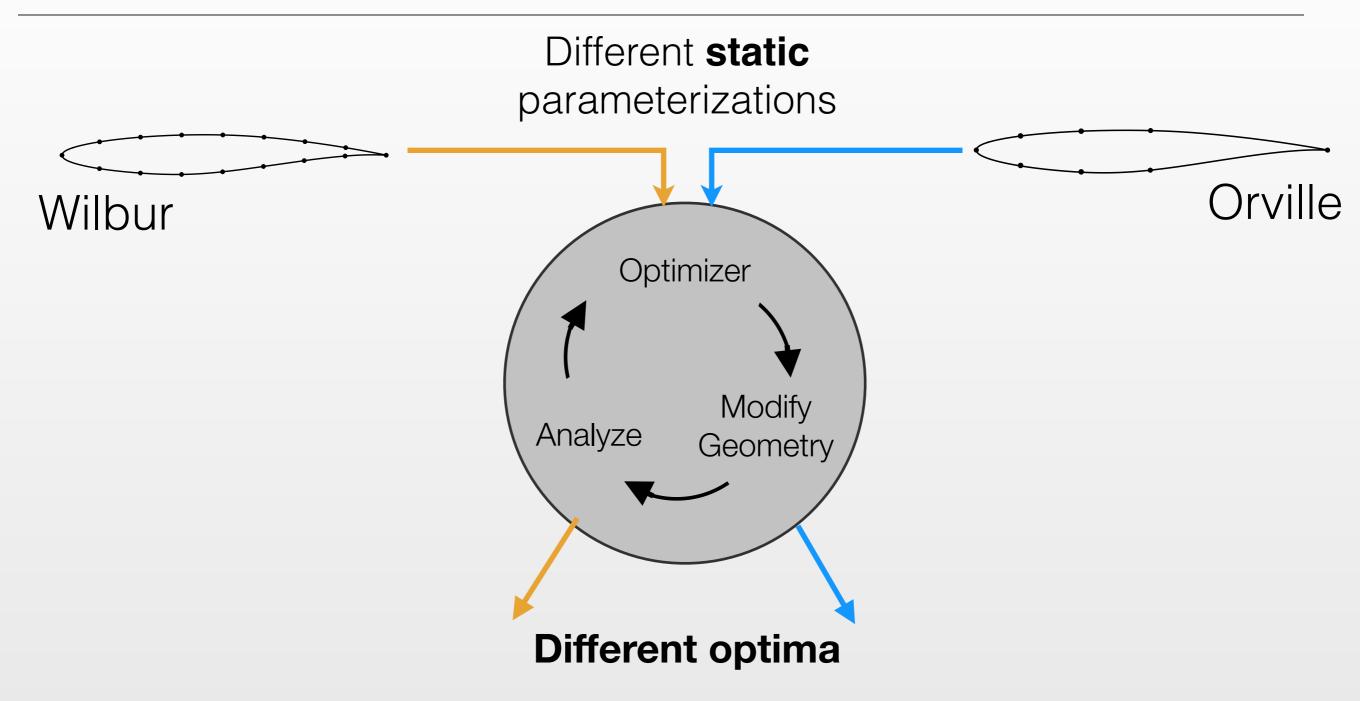
3

#### Shape Parameterization



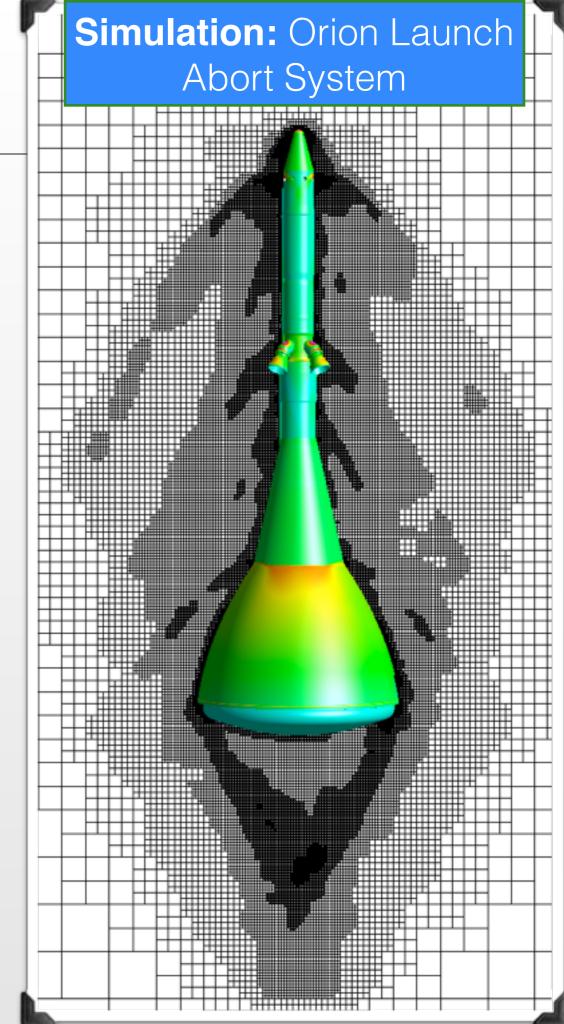
- Shape parameterization reduces continuous design space into finite search space
- Reduces range of reachable shapes

#### Static Parameterization



# Motivation

- Design of complex vehicles in unfamiliar settings, driven by highfidelity simulations.
- Choice of shape parameters impacts:
  - Bias towards familiar designs.
  - Ability to approximate the continuous optimal solution. (Want *more* DOF)
  - Optimization cost. (Want fewer DOF)





#### **Research Goal:**

Develop system for automatic, adaptive shape parameterization refinement during optimization

#### **Requirements:**

- Gradually approach continuous optimum (convergent)
- Without a priori knowledge (automated)
- Using as few design variables as possible (adaptive)

## Previous Work

# **Progressive** (uniform "h"-refinement)

#### Gradually increase resolution

- (1991) Kohli and Carey Multifidelity shape representation for structural optimization
- (1993) Marco et al. Aerodynamic optimization with nested parameters

#### **Redistribution** (*"r"-refinement*)

- Improve distribution of shape control
- (2004, 2006) Desideri and El Majd, Duvigneau — Minimize total variation of Bezier/FFD control points
- ◆(2012) Hwang and Martins Equally distribute arc-length of curve between B-spline control points

These approaches are **insensitive to the** goals of aerodynamic optimization.

#### Towards **goal-oriented** adaptation:

- •(2011) Han and Zingg Discrete refinement approach
  - **Restrictions:** Single-component design, only localized constraints, can only add one new variable at a time
- (2014) Poole and Allen Redistribution approach
  - Restrictions: Only geometric matching of airfoils
- (2015) Anderson Discrete adaptation approach appropriate for general aerodynamic design problems

# Contributions

- Complete **system** for automatic, adaptive parameterization
- Novel **refinement indicator** that enables adaptive parameterization for general problems:
  - Multiple components
  - Multiple classes of shape control
  - High curvature variation in design space
  - General constraints
- Several new algorithms and strategies to accelerate and automate adaptation
- First verification of robust convergence of adaptation
- Implementation, testing in a production design environment

## Outline

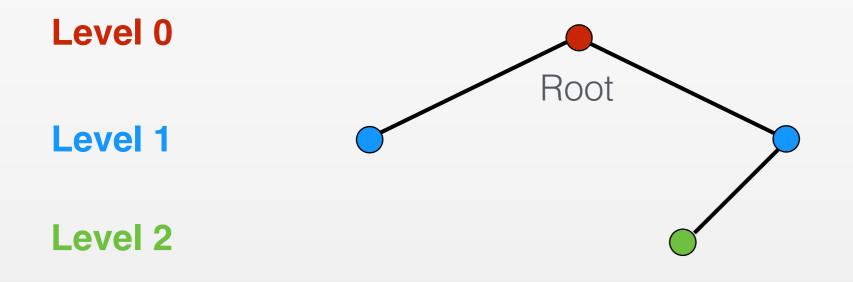
#### ✓ Introduction

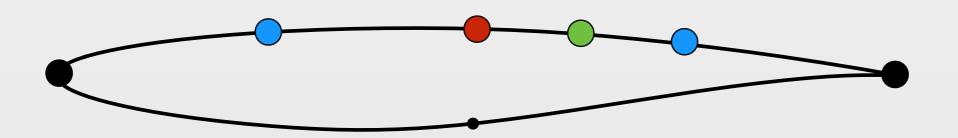
#### Adaptive Parameterization

- Discrete Adaptation (How?)
- Refinement Indicator (Where?)
- Adaptation Strategy
- Verification
- Design Examples

### Shape Control Refinement

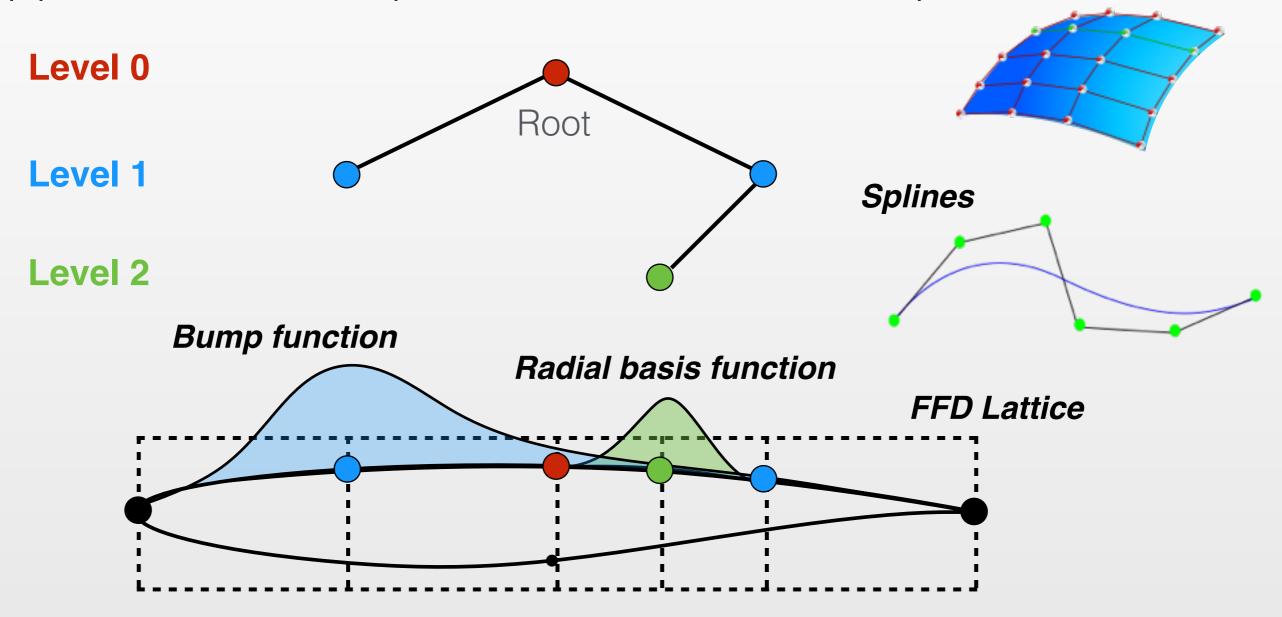
View shape parameterization as **binary tree**:





# Shape Control Refinement

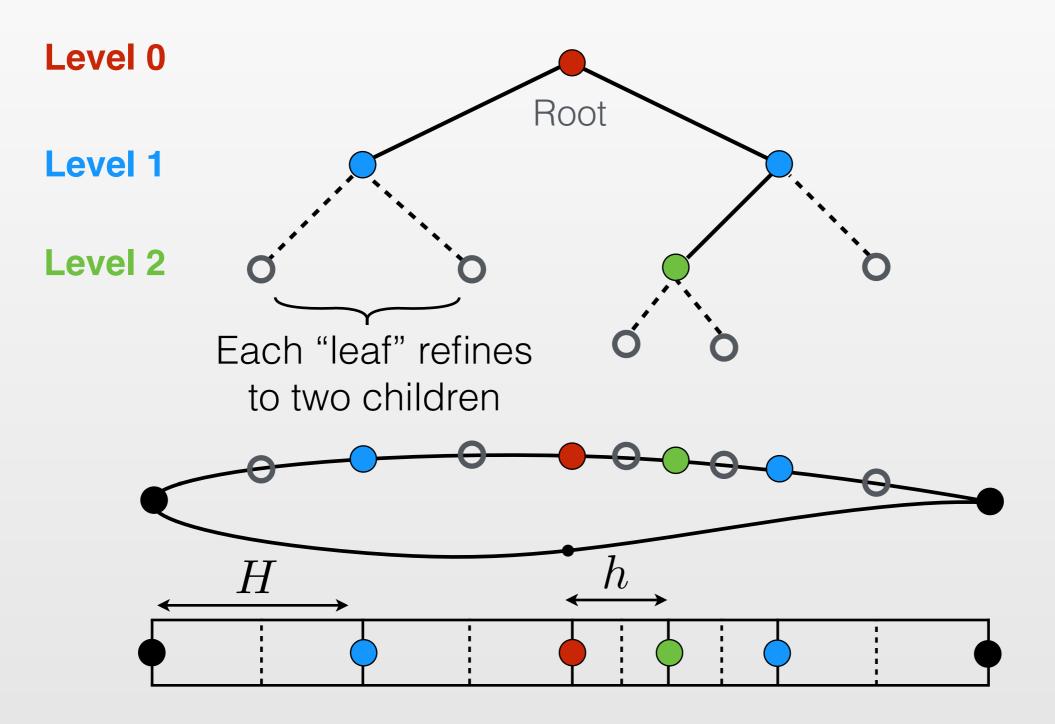
Applicable to most parameterization techniques



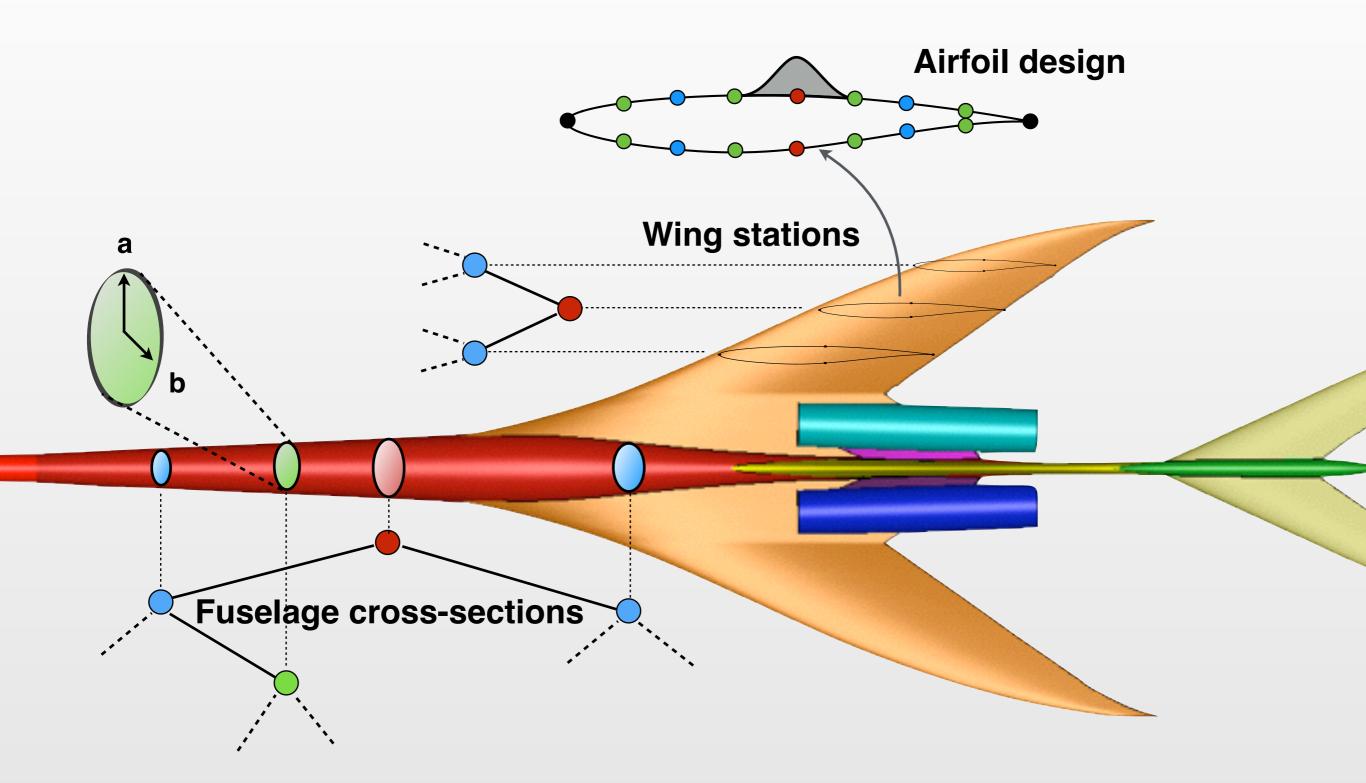
**NURBS** 

# Shape Control Refinement

View shape parameterization as **binary tree**:



## Configuration Design



## Outline

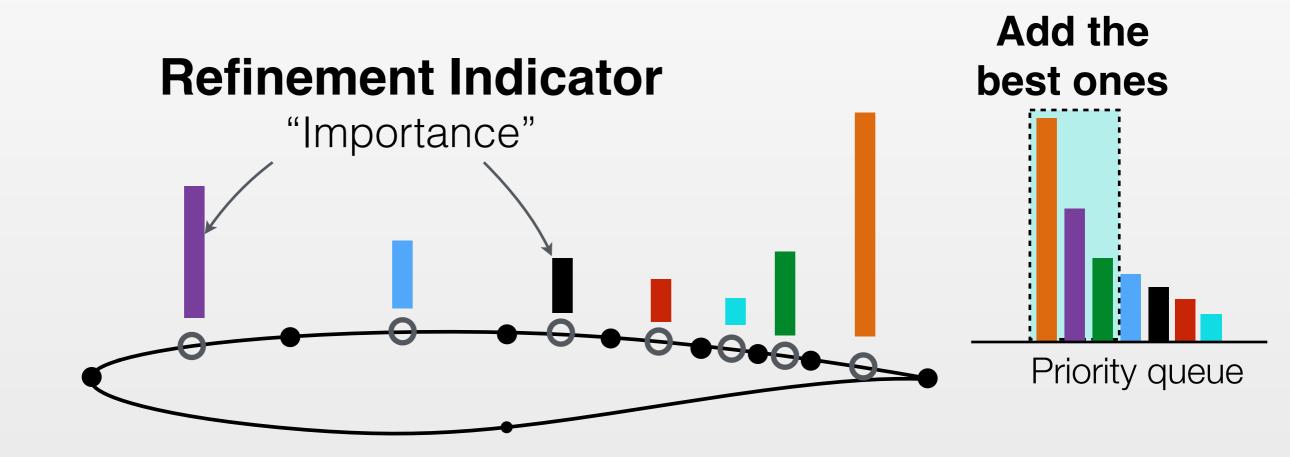
#### ✓ Introduction

#### Adaptive Parameterization

- ✓ Discrete Adaptation
- Refinement Indicator
- Adaptation Strategy
- Verification
- Design Examples

#### Adaptive Refinement

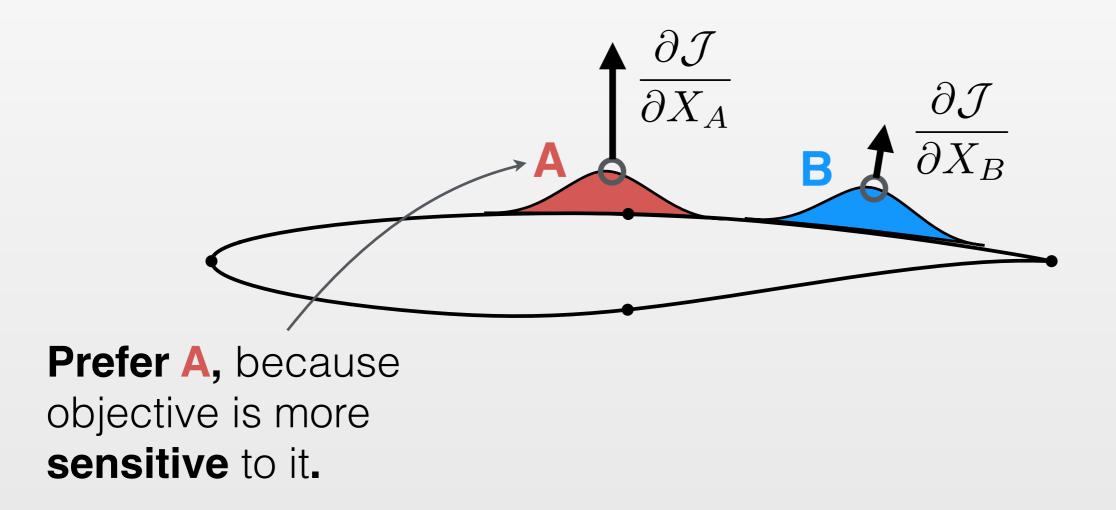
**Goal:** Determine **most important** candidate parameters



#### Previous Approach

18

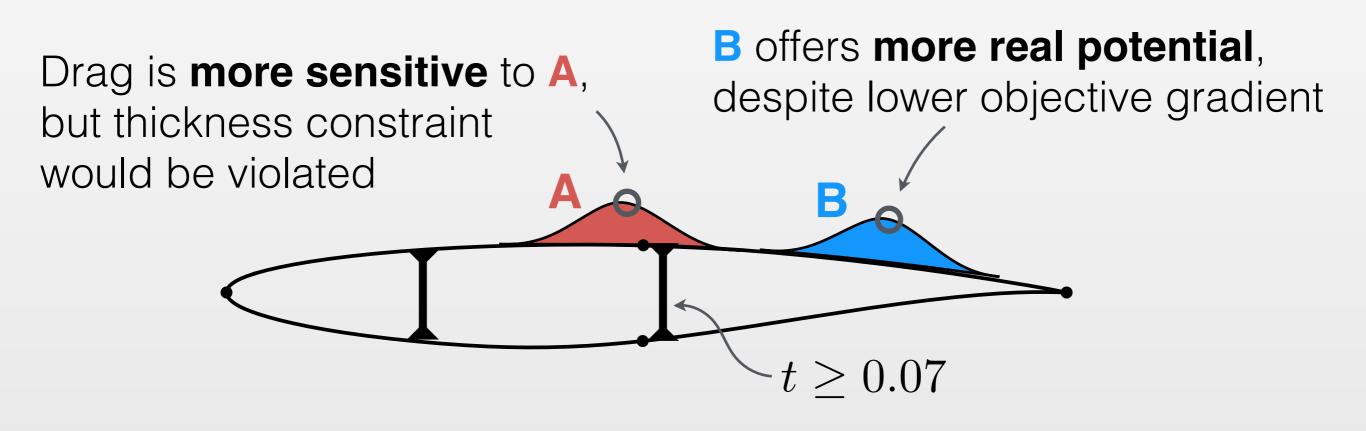
 (2011) Han and Zingg rank parameters by magnitude of objective gradient with respect to candidate design variables.<sup>†</sup>



<sup>†</sup> (2011) X. Han, D. Zingg. "An Evolutionary Geometry Parametrization for Aerodynamic Shape Optimization." AIAA 2011-3536

#### Ignores constraints

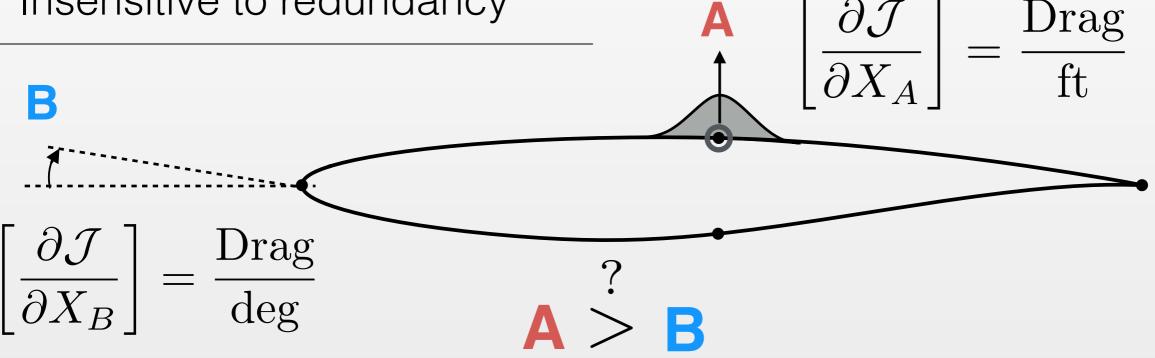
Inconsistent units Ignores curvature variation Insensitive to redundancy

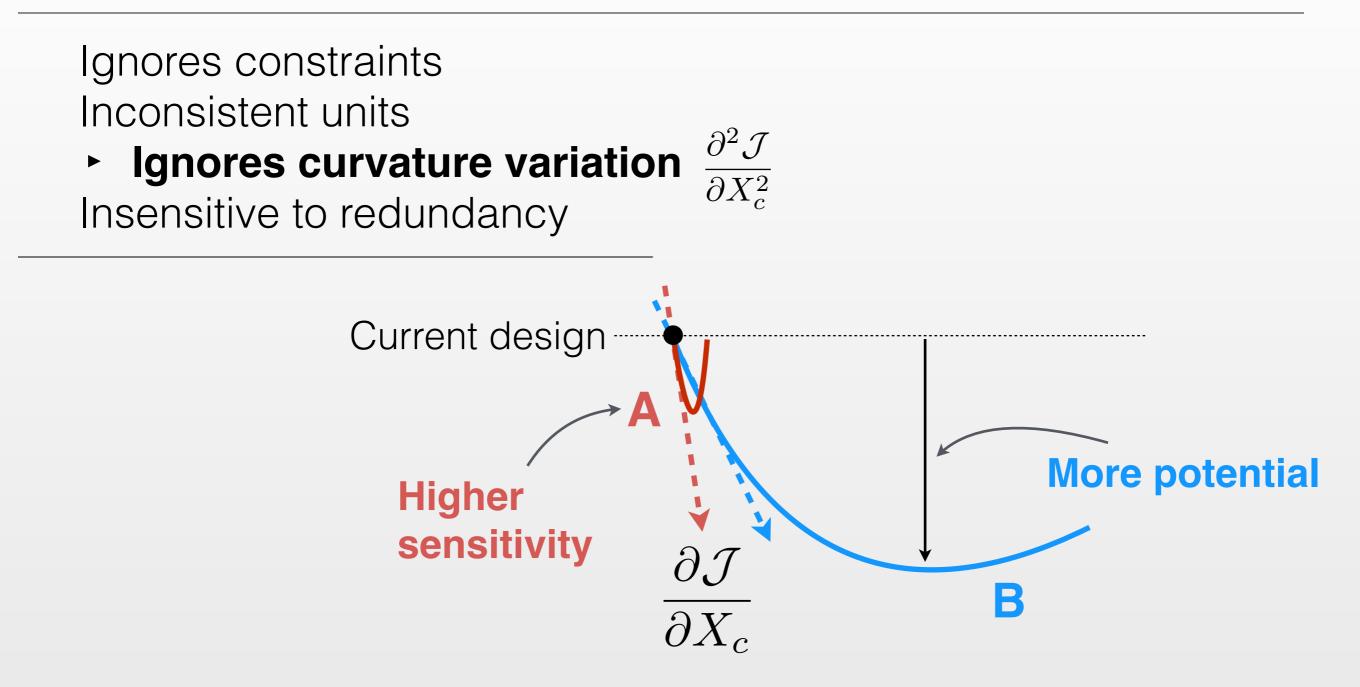


Ignores constraints

Inconsistent units

Ignores curvature variation Insensitive to redundancy

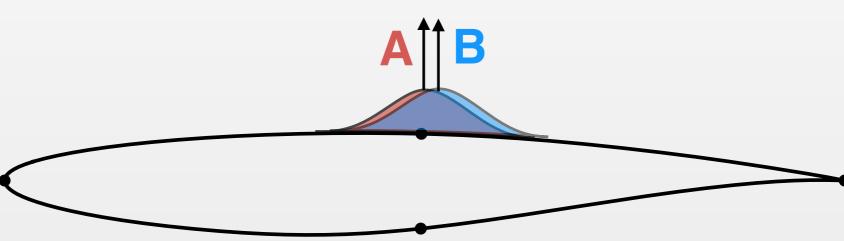




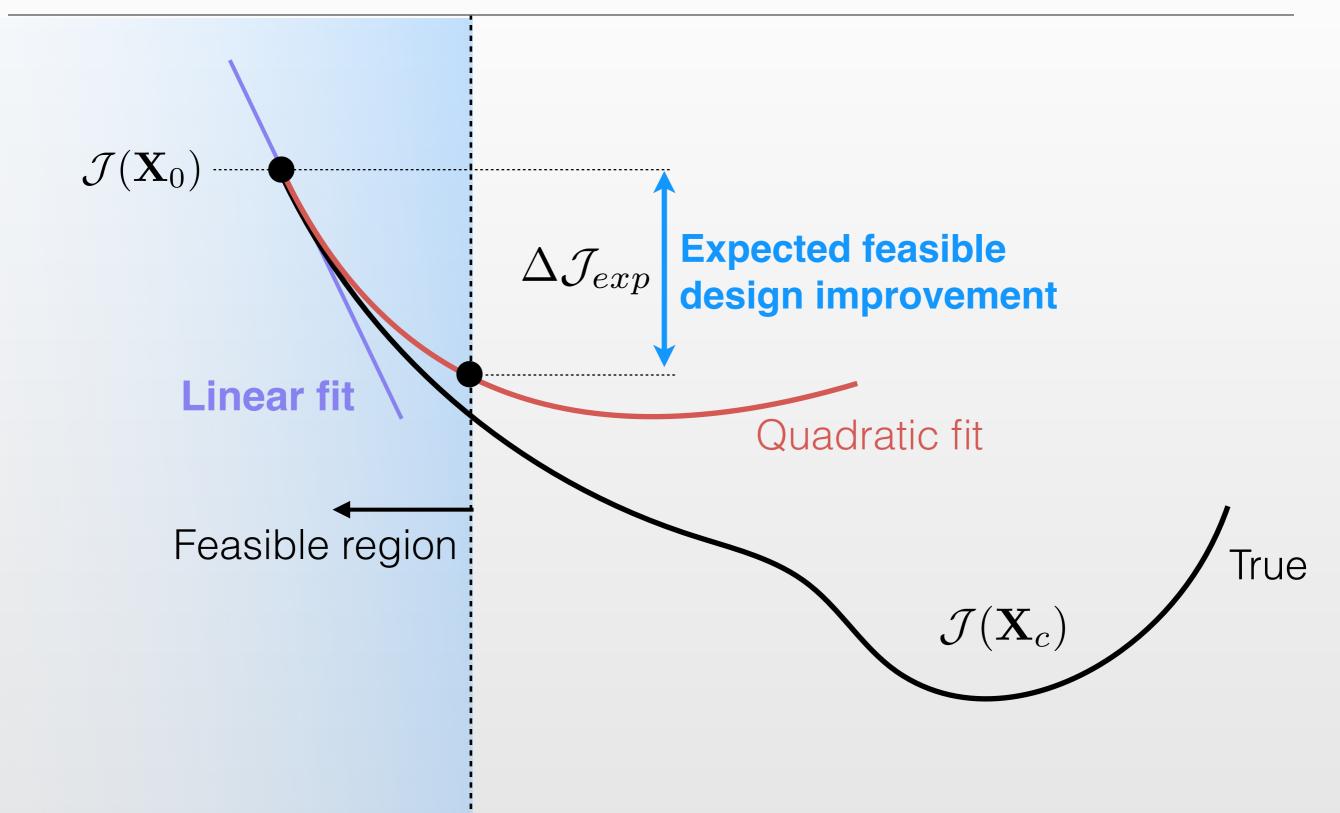
Ignores constraints Inconsistent units Ignores curvature variation

Insensitive to redundancy

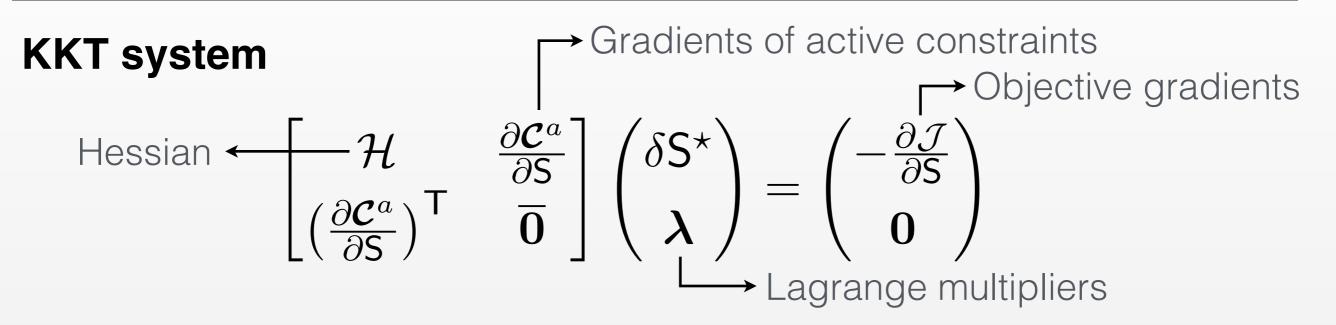
# Either one would be useful, but not both



#### New Refinement Indicator



#### Expected Feasible Design Improvement



Solve for Newton step to predicted optimum

$$\delta S^{\star} = -\mathcal{H}^{-1} \left( \frac{\partial \mathcal{J}}{\partial S} + \lambda \frac{\partial \mathcal{C}^{a}}{\partial S} \right) \xrightarrow{\text{Gradient}} \text{Gradient}$$

$$uadratic \text{ Taylor expansion} \xrightarrow{\text{Hessian}} \text{Hessian}$$

$$\mathcal{J}(S_{0} + \delta S) \approx \mathcal{J}(S_{0}) + \left\langle \frac{\partial \mathcal{J}}{\partial S}, \delta S \right\rangle + \frac{1}{2} \left\langle \mathcal{H} \delta S, \delta S \right\rangle + \dots$$

# **Refinement Indicator**

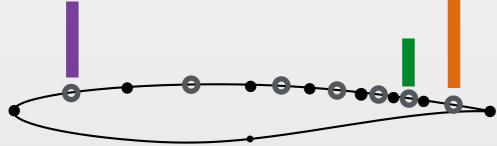
$$\Delta \mathcal{J}_{exp}^{\infty} = \frac{1}{2} \left\langle \left( \frac{\partial \mathcal{J}}{\partial \mathsf{S}} + \boldsymbol{\lambda} \frac{\partial \mathcal{C}^{a}}{\partial \mathsf{S}} \right), \mathcal{H}^{-1} \left( \frac{\partial \mathcal{J}}{\partial \mathsf{S}} + \boldsymbol{\lambda} \frac{\partial \mathcal{C}^{a}}{\partial \mathsf{S}} \right) \right\rangle$$

Expected feasible objective reduction in **candidate** search space:

**KKT stationarity** 0 at optimum

$$I \equiv \Delta \mathcal{J}_{exp}^{\infty} = \frac{1}{2} \left\langle \left( \frac{\partial \mathcal{J}}{\partial \mathbf{X}_c} + \boldsymbol{\lambda} \frac{\partial \mathcal{C}^a}{\partial \mathbf{X}_c} \right), (\mathcal{M}\mathcal{H})^{-1} \left( \frac{\partial \mathcal{J}}{\partial \mathbf{X}_c} + \boldsymbol{\lambda} \frac{\partial \mathcal{C}^a}{\partial \mathbf{X}_c} \right) \right\rangle$$

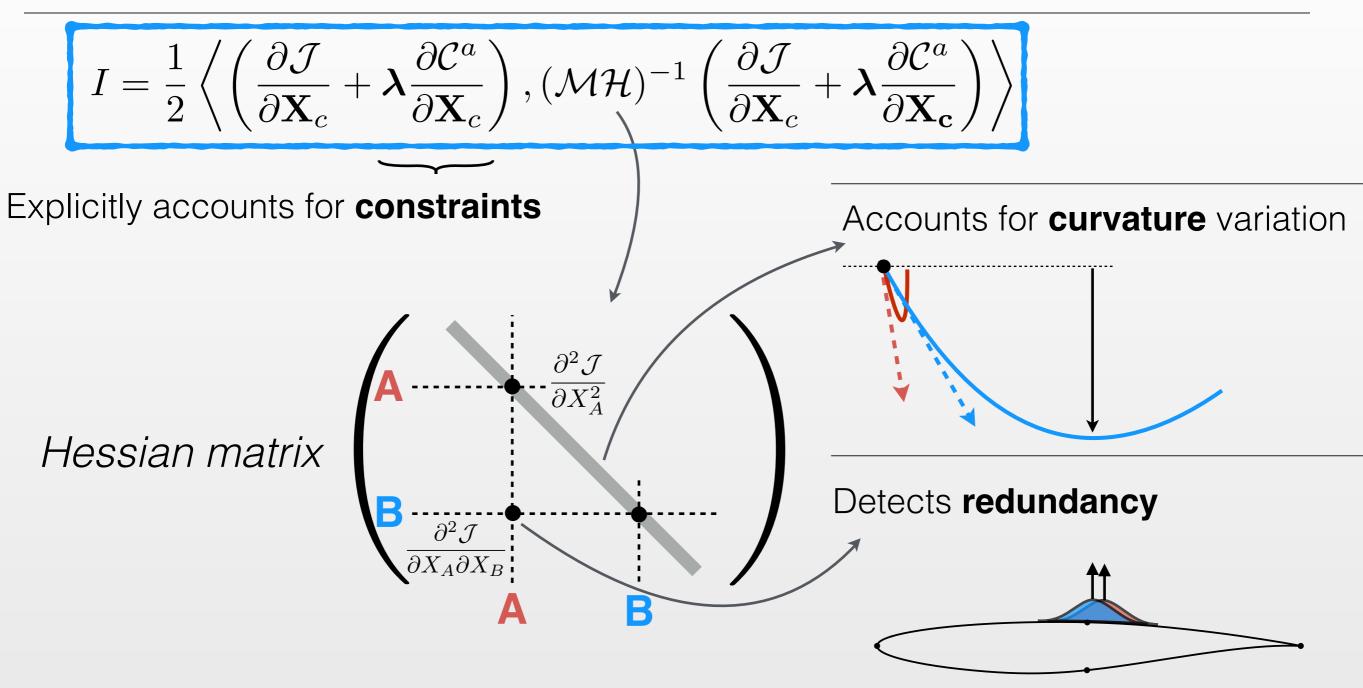
Use as **refinement indicator** 



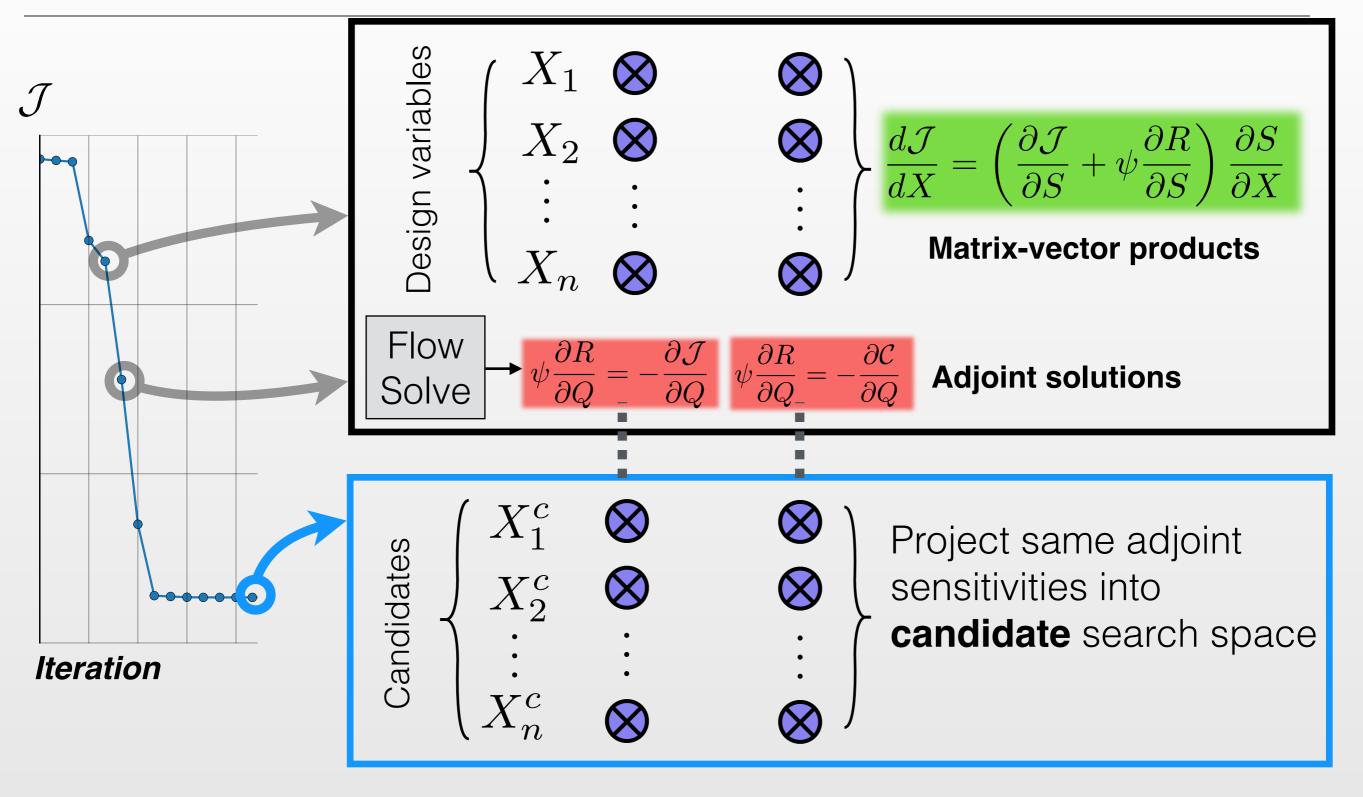
Has sensible **units**  $[I] = \frac{\text{Drag}}{\text{ft}} \left(\frac{\text{ft}^2}{\text{Drag}}\right) \frac{\text{Drag}}{\text{ft}} = \text{Drag}$ 

"expected drag reduction"

## **Refinement Indicator**



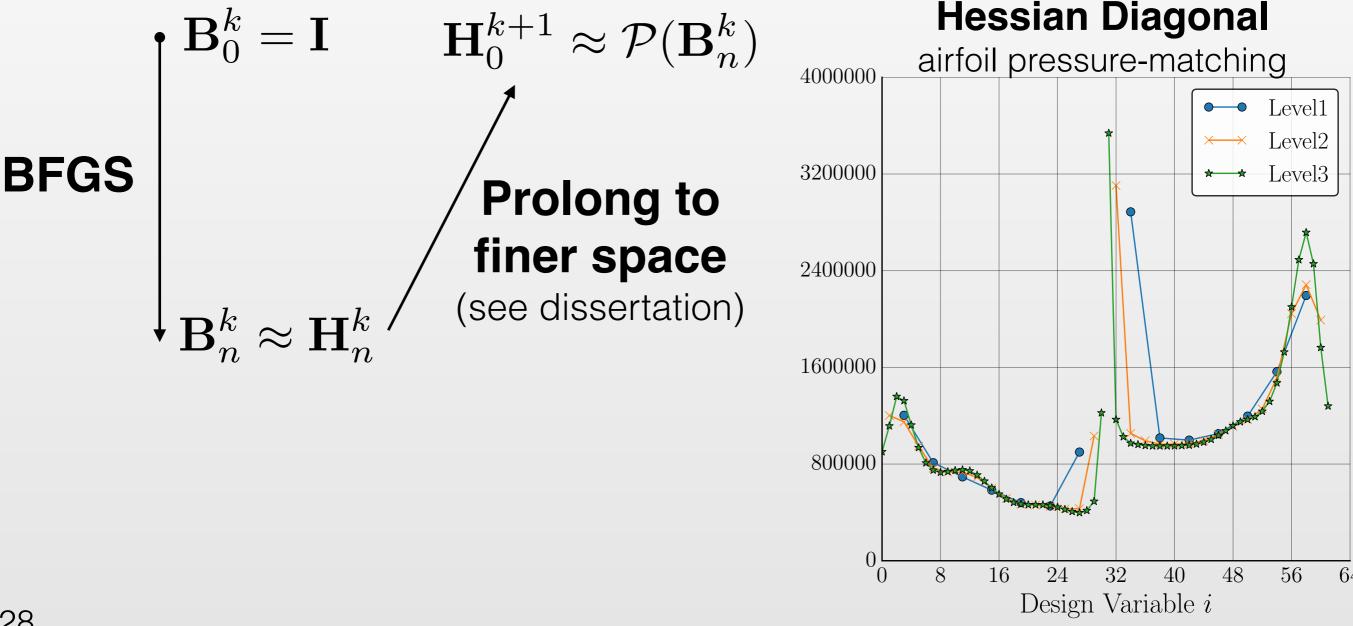
#### Indicator Computation — Gradients



#### Indicator Computation — Hessian Estimation

$$I = \frac{1}{2} \left\langle \left( \frac{\partial \mathcal{J}}{\partial \mathbf{X}_c} + \boldsymbol{\lambda} \frac{\partial \mathcal{C}^a}{\partial \mathbf{X}_c} \right), (\mathcal{M}\mathcal{H})^{-1} \left( \frac{\partial \mathcal{J}}{\partial \mathbf{X}_c} + \boldsymbol{\lambda} \frac{\partial \mathcal{C}^a}{\partial \mathbf{X}_c} \right) \right\rangle$$

**Estimate** Hessian from **quasi-Newton** approximation in previous space



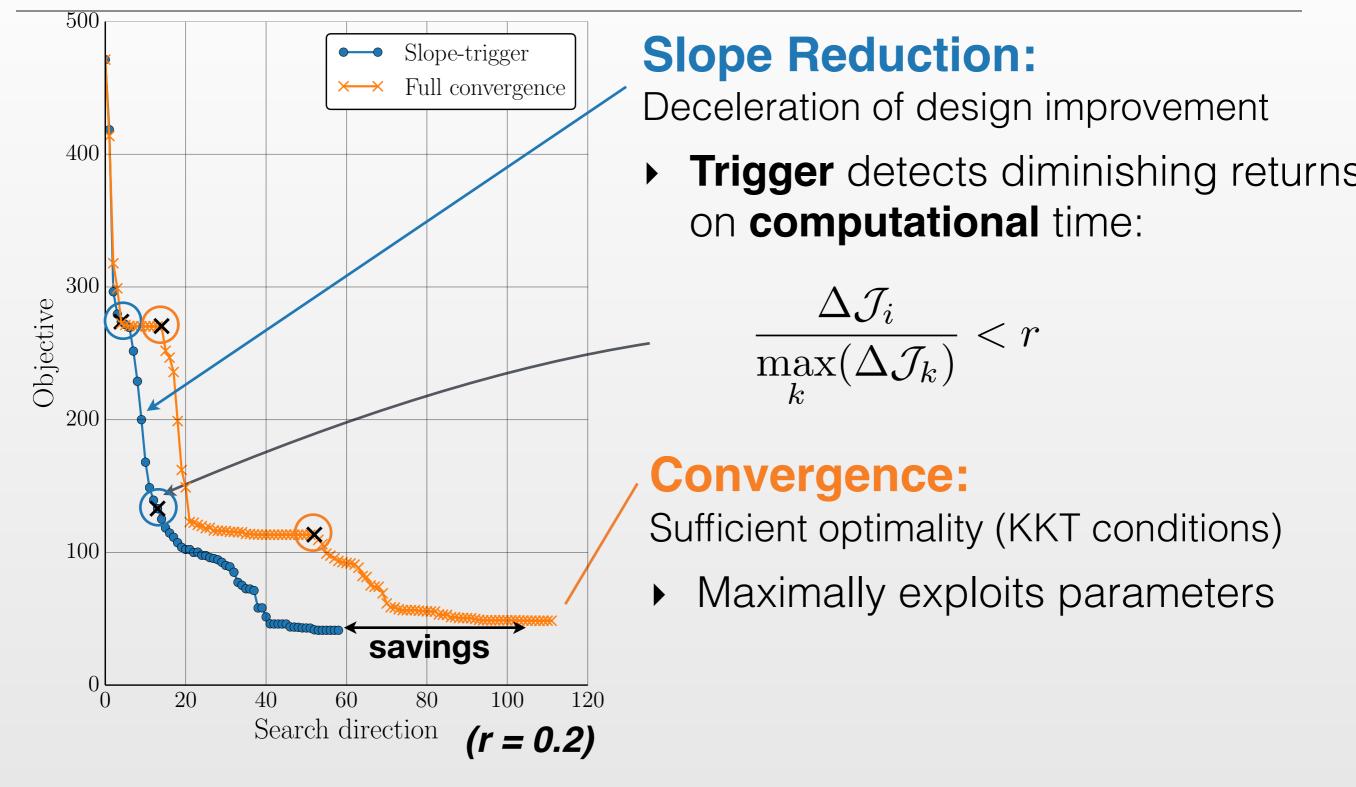
## Outline

#### ✓ Introduction

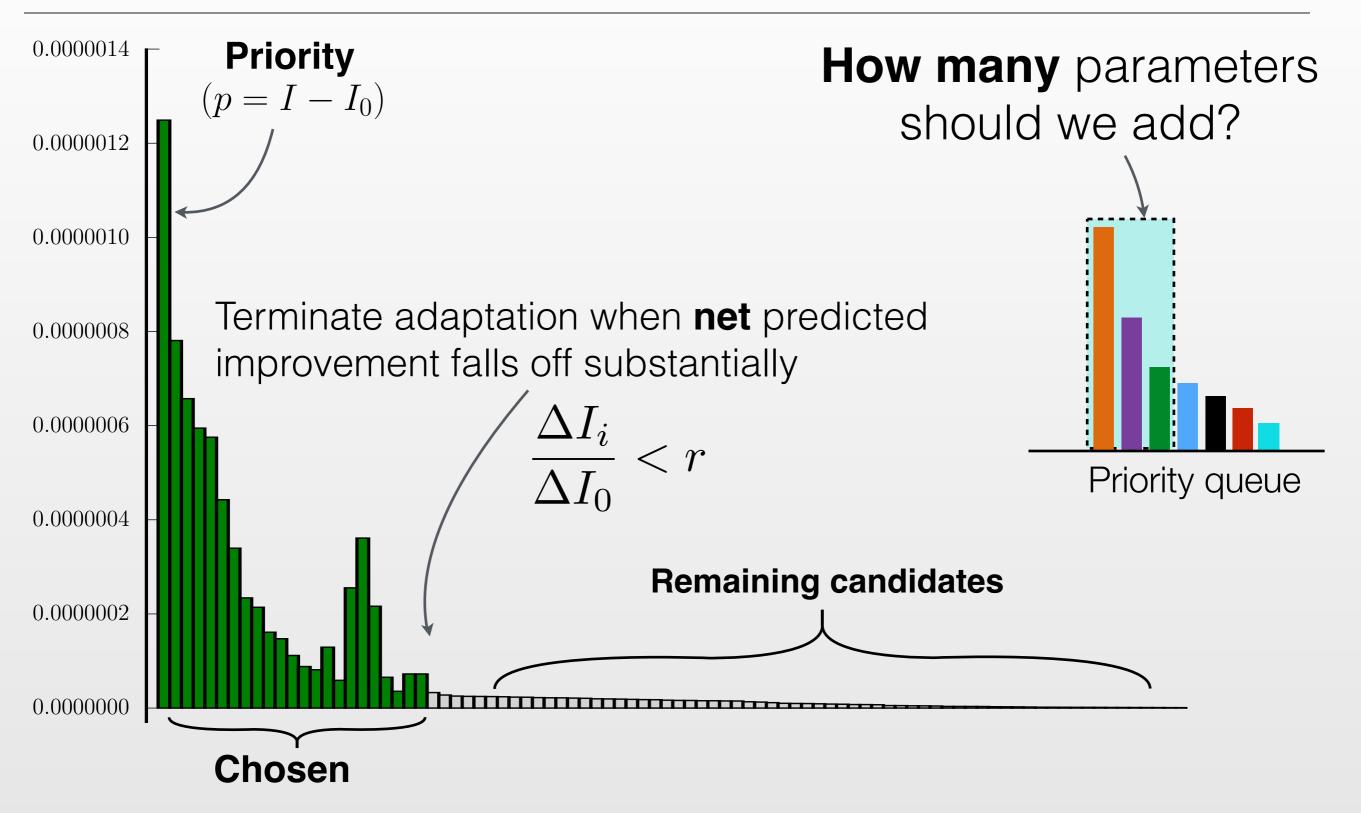
#### Theory and Approach

- ✓ Discrete Adaptation
- ✓ Refinement Indicator
- Adaptation Strategy
- Verification
- Design Examples

# When to refine?

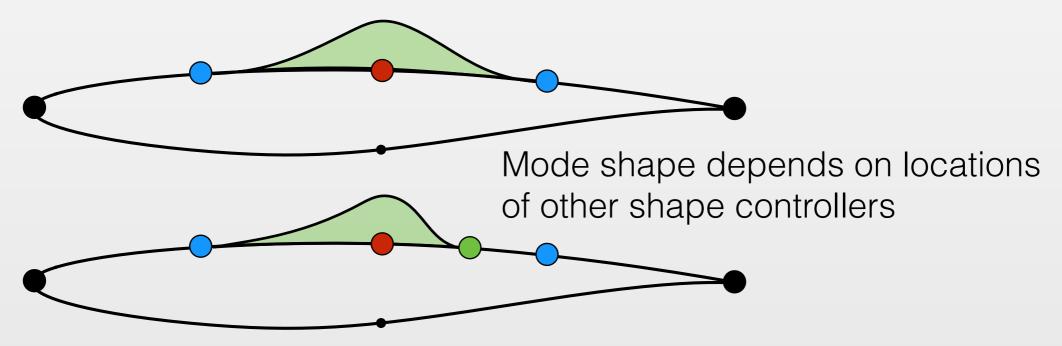


## Growth rate



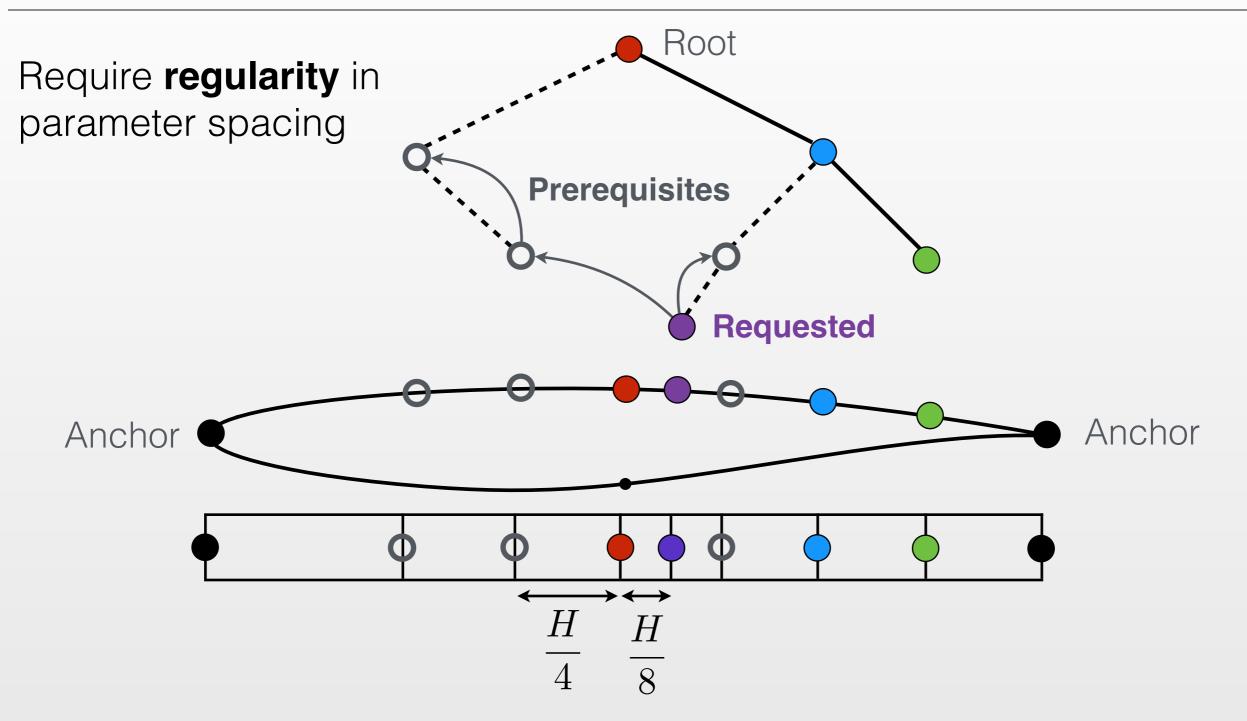
# Adding Multiple Parameters

- Adaptation: "Find the best N out of M parameters"
- Properly a **combinatorial optimization** problem
  - Not separable for most deformers
  - But conducive to approximate solutions
- I use an approximate constructive (greedy) algorithm<sup>†</sup>



<sup>†</sup> (2015) **Anderson**, G.R., Aftosmis, M. J. "Adaptive Shape Control for Aerodynamic Design." AIAA 2015-0398

# Regularity



# Outline

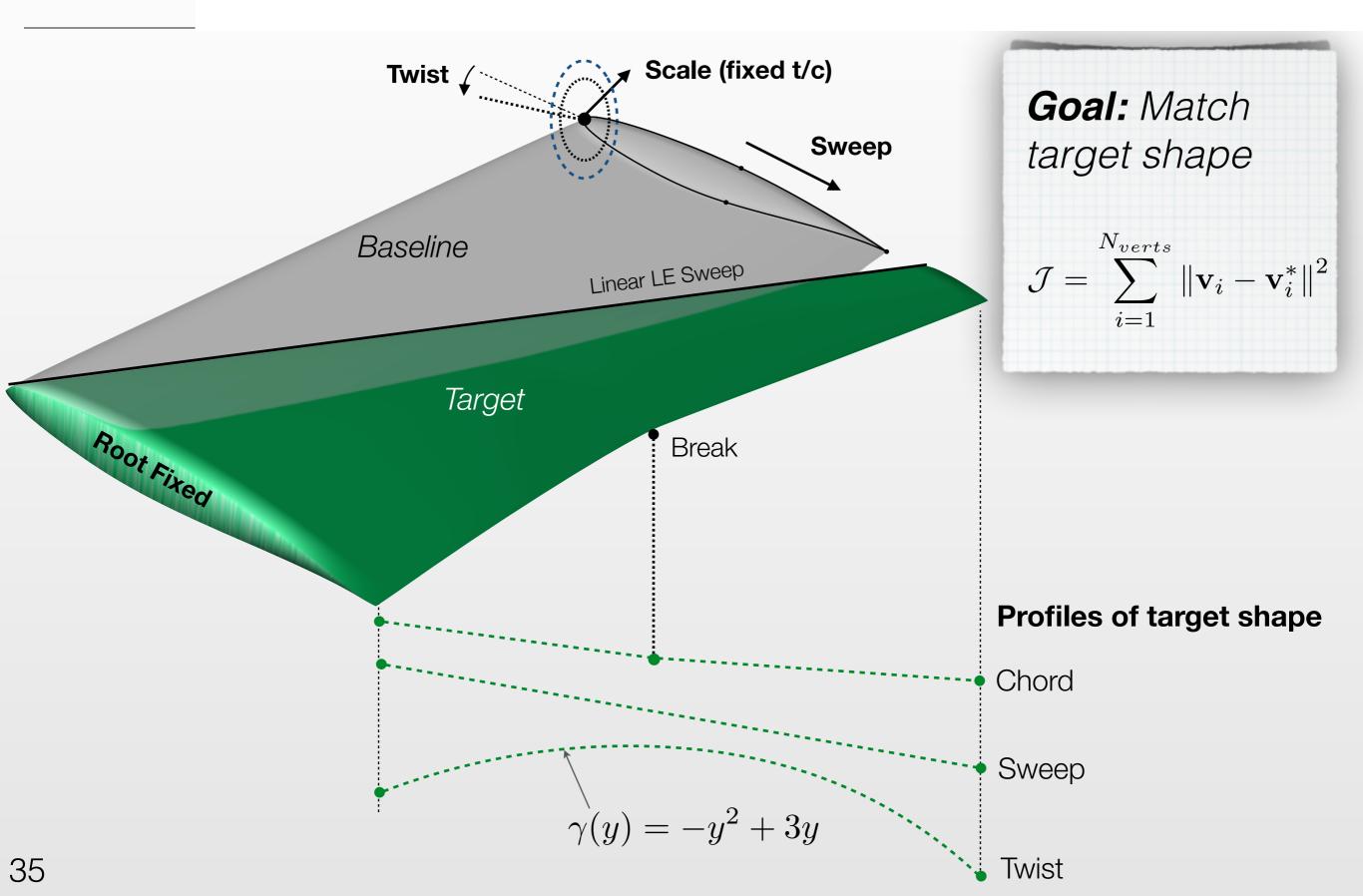
#### ✓ Introduction

#### ✓ Theory and Approach

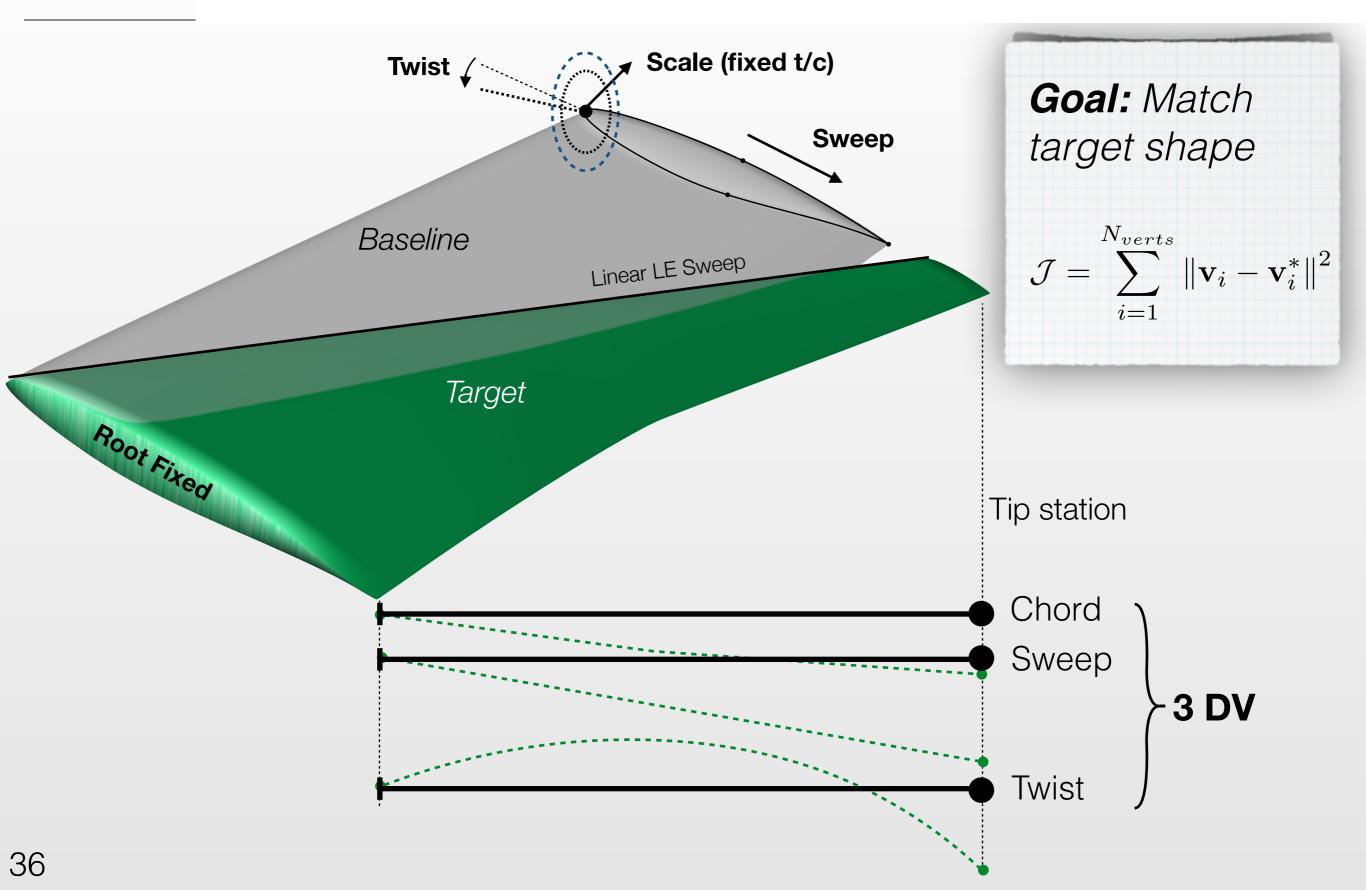
#### Verification

- Correctness Does the indicator predict actual design improvement?
- Robustness Does the approach always converge to the continuous optimum?
- Design Examples

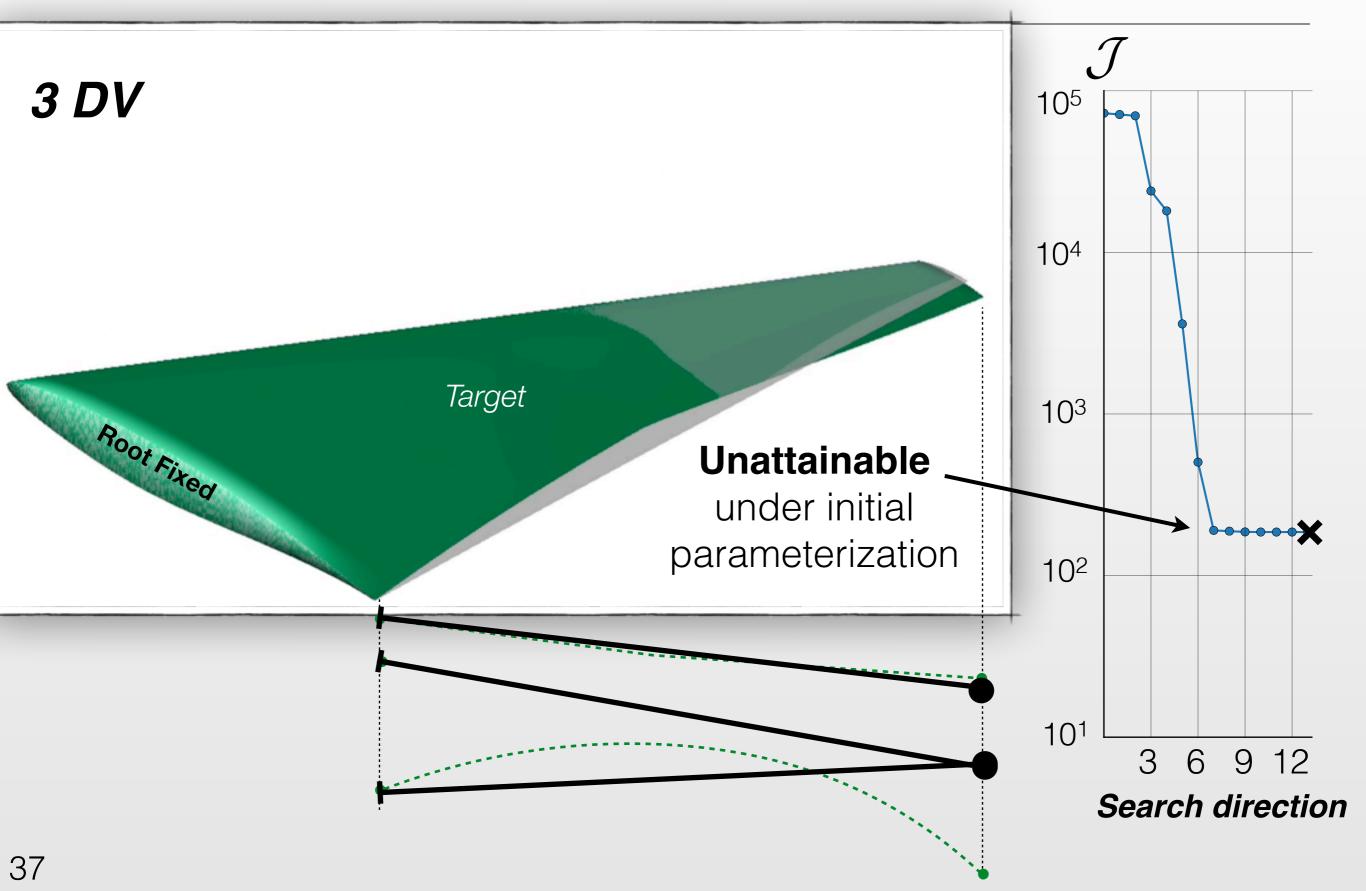
#### Verificat

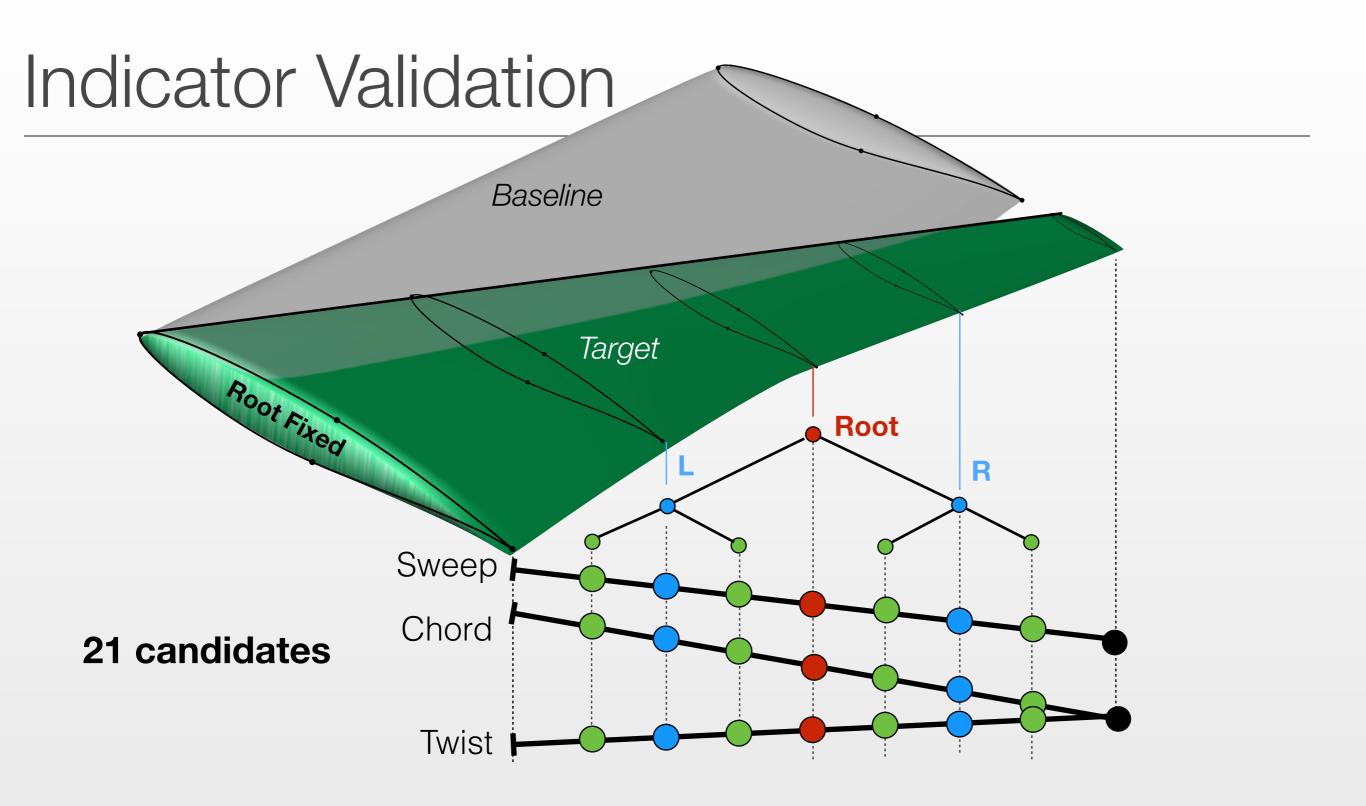


#### Initial F



#### Shape Matching under Initial Parameterization





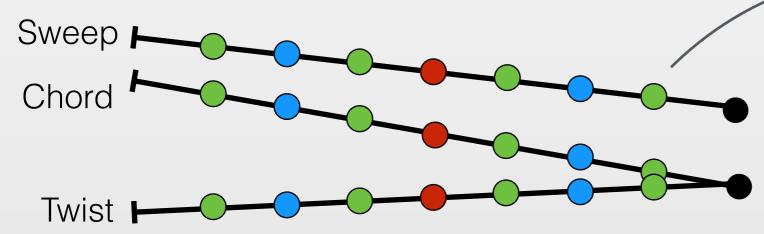
# Indicator Validation

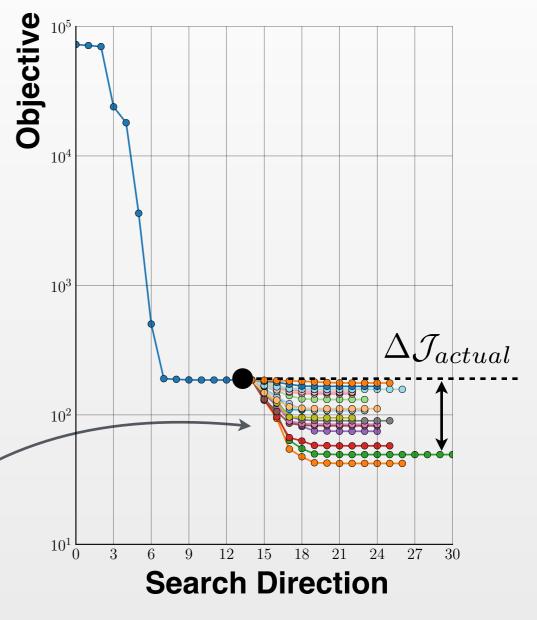
For each candidate:

1. **Predict** design improvement. With indicator:

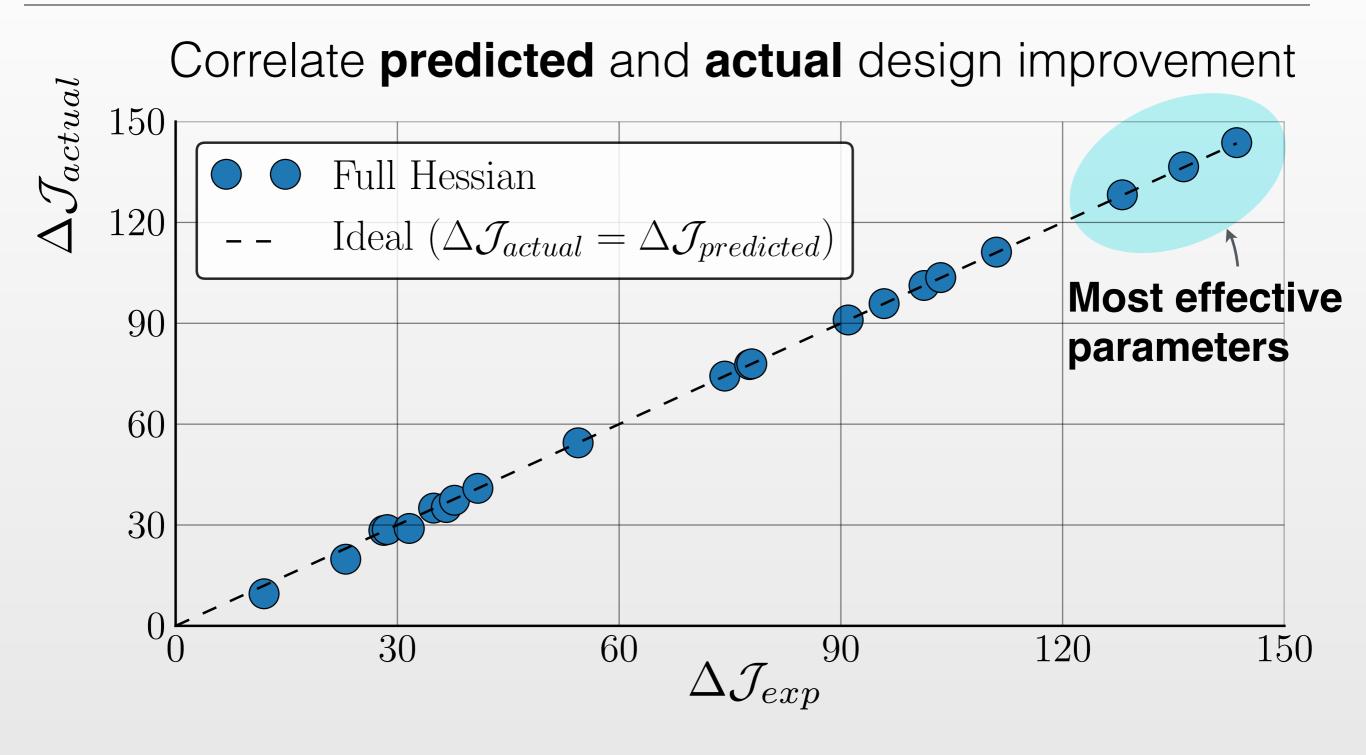
$$I = \frac{1}{2} \left\langle \left( \frac{\partial \mathcal{J}}{\partial \mathbf{X}_c} + \boldsymbol{\lambda} \frac{\partial \mathcal{C}^a}{\partial \mathbf{X}_c} \right), (\mathcal{M}\mathcal{H})^{-1} \left( \frac{\partial \mathcal{J}}{\partial \mathbf{X}_c} + \boldsymbol{\lambda} \frac{\partial \mathcal{C}^a}{\partial \mathbf{X}_c} \right) \right\rangle$$

2. Measure **actual** improvement. Run optimization for each candidate.

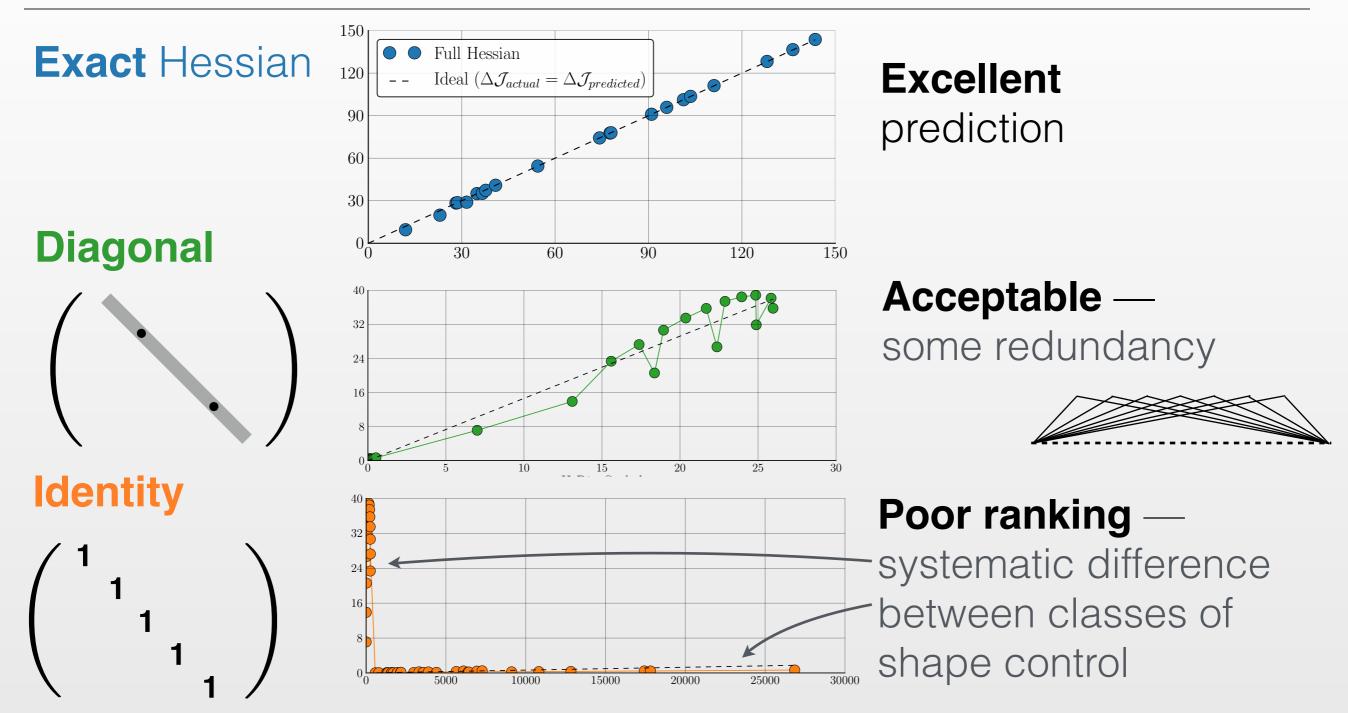




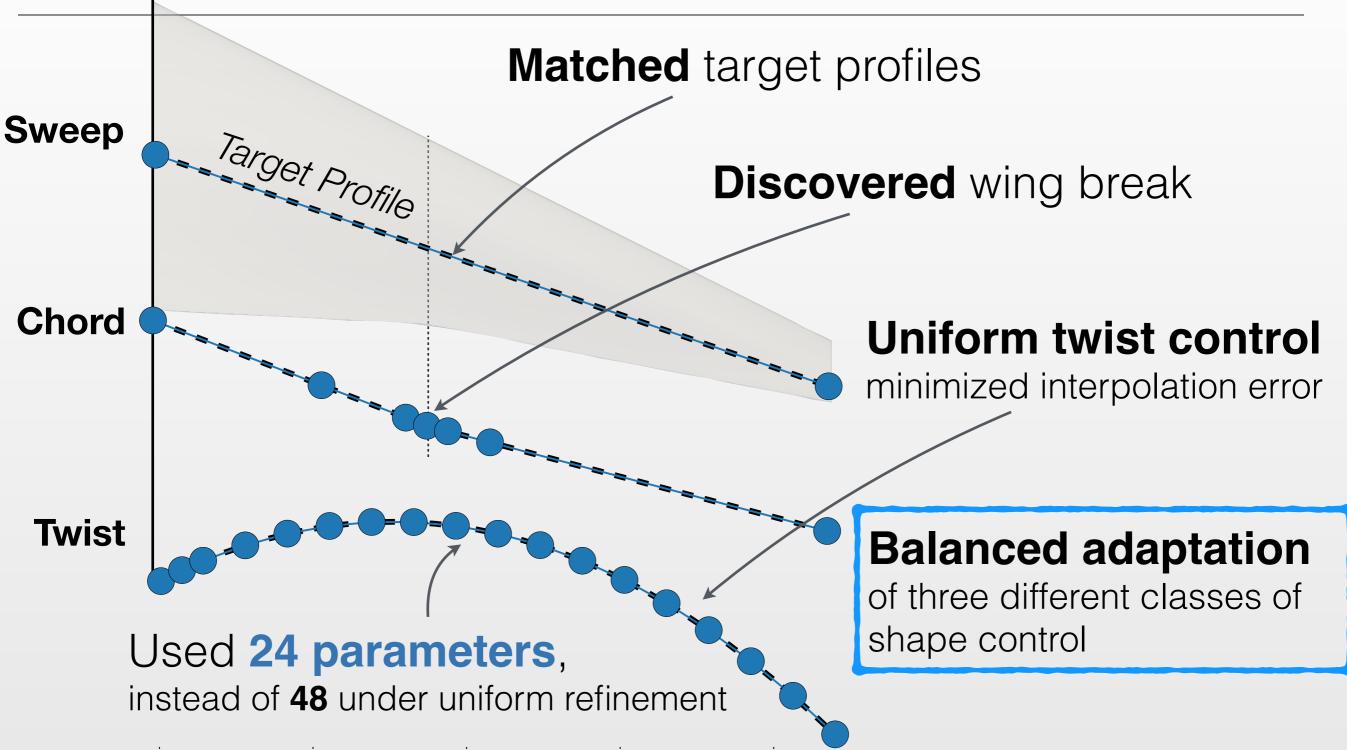
### Indicator Validation



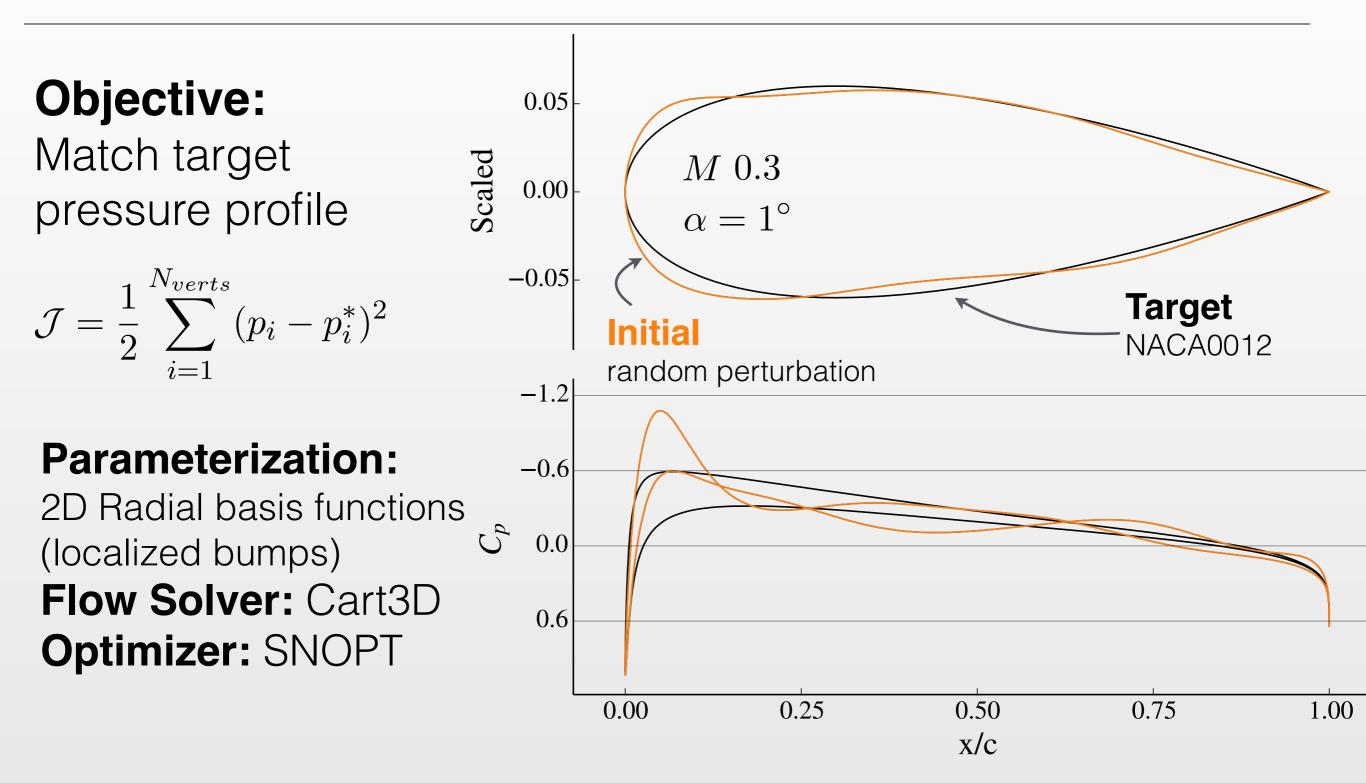
# Approximations

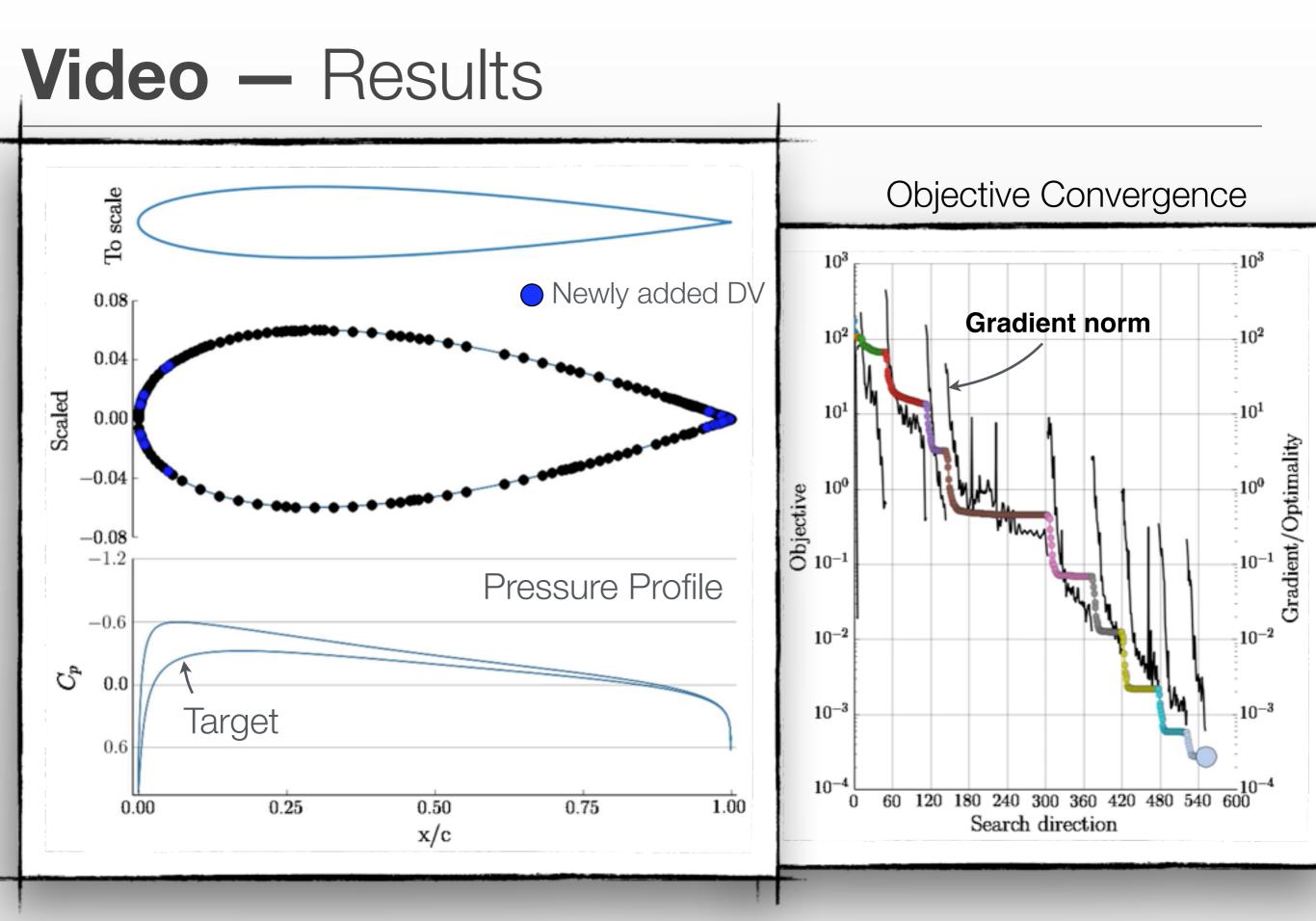


### Recovery of Necessary Parameters

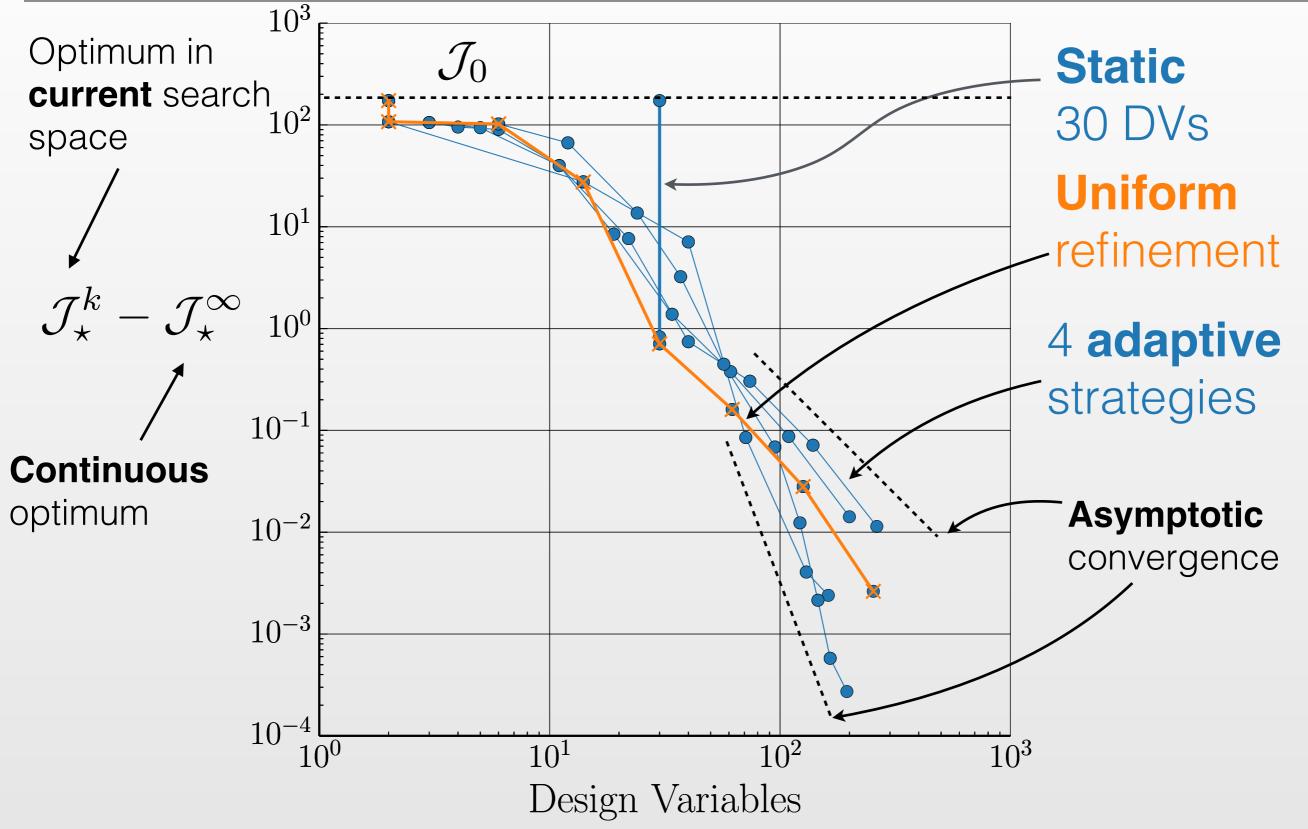


#### Verification Study 2: Pressure Signature Matching

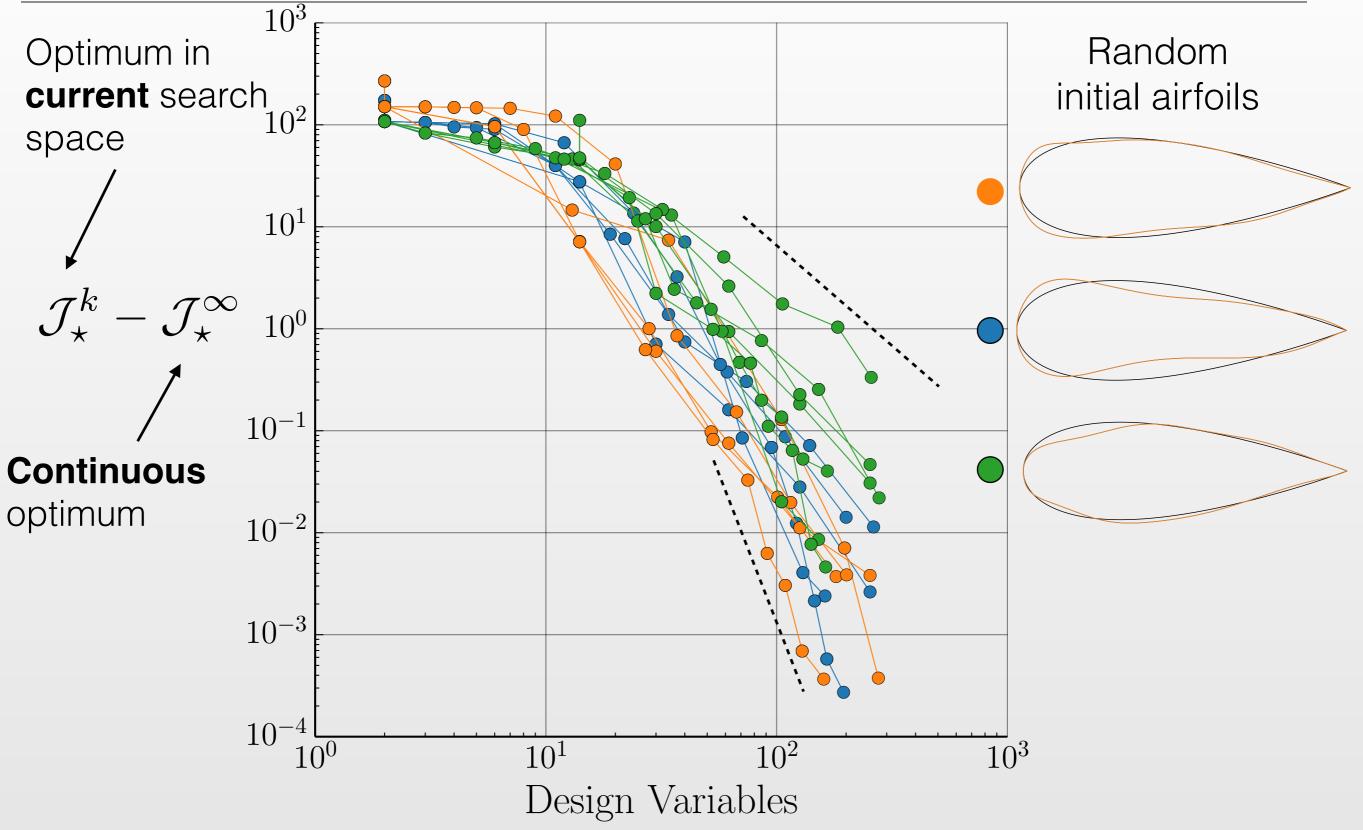




### Convergence to Continuous Optimum



### Convergence to Continuous Optimum



### Convergence Rate

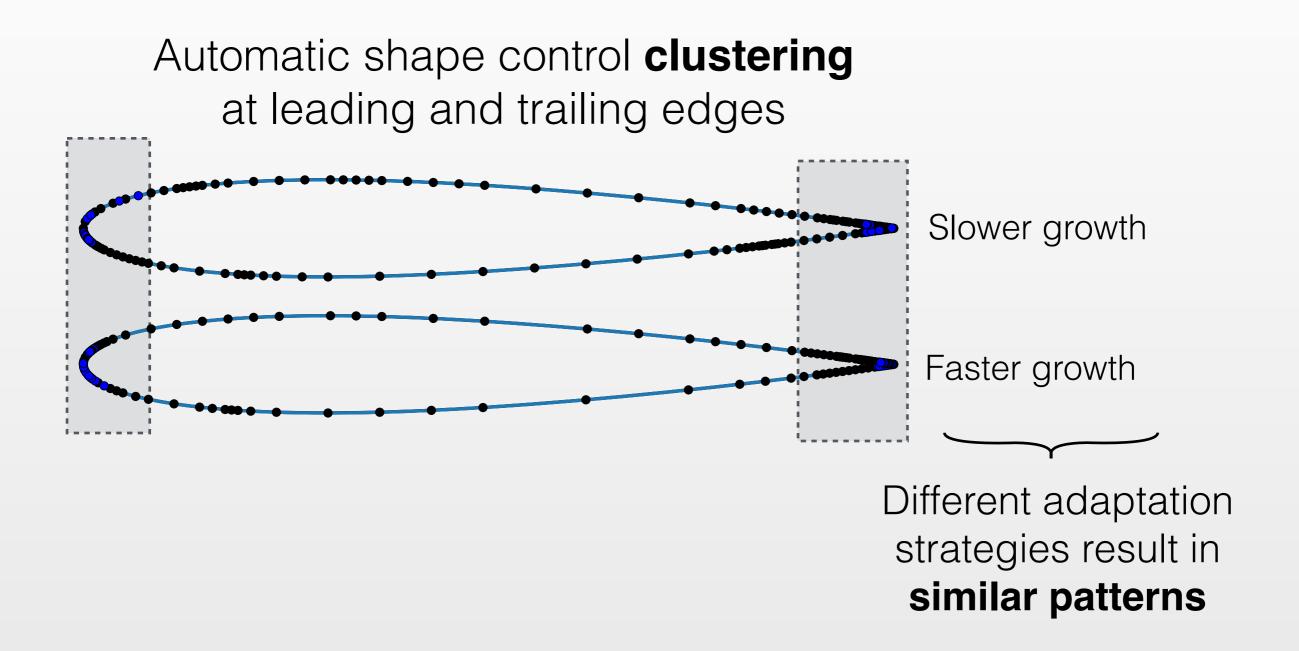
#### Efficient in use of design variables

Asymptotic convergence rate of  $\mathcal{J}^k_\star - \mathcal{J}^\infty_\star$ 

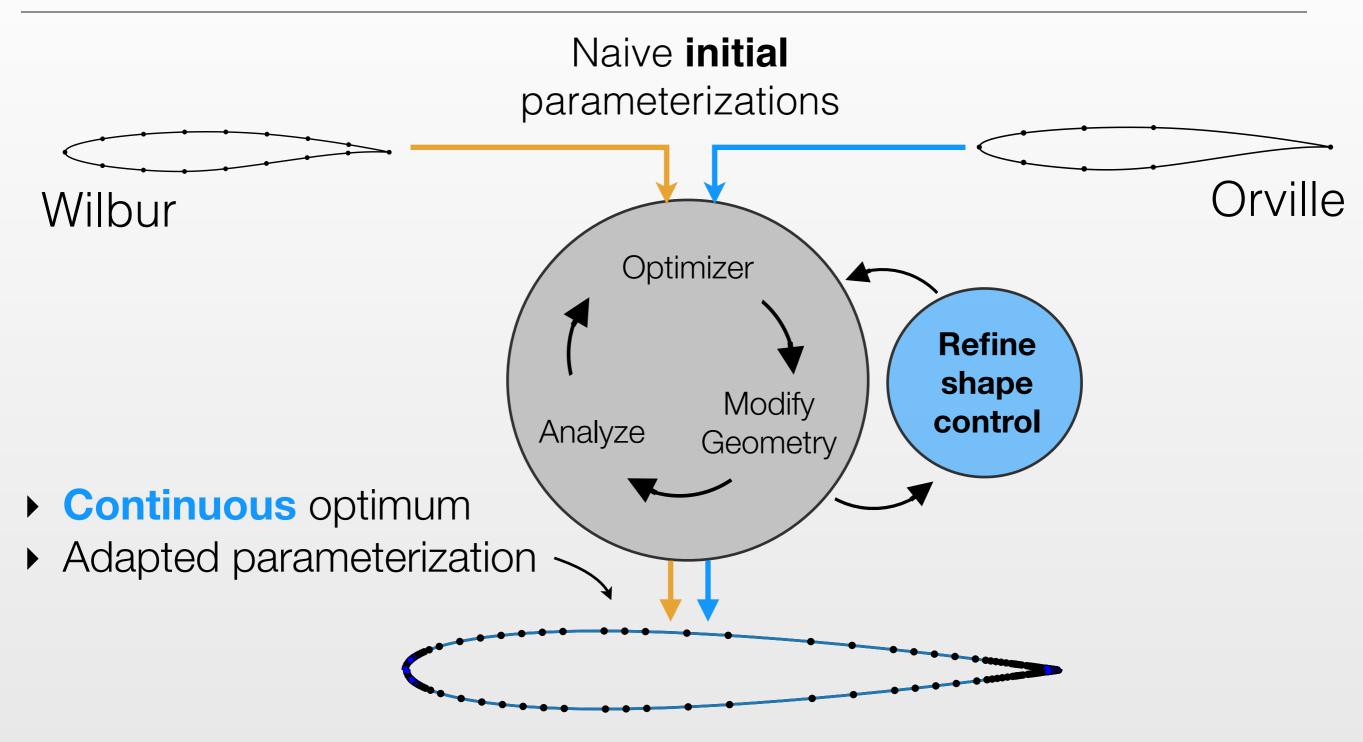
	Uniform	Adaptive	
Case		Strategy 1	Strategy 2
1	2.6	8.3	5.0
2	2.4	5.2	5.6
3	2.7	5.7	4.7
mean	2.6	5.75	
$\frac{\Delta \mathcal{J}}{\Delta N_{DV}} *$	$\sim 6 imes$	$\sim {f 54}  imes$	

\* Reduction in objective for  $2 \times$  increase in  $N_{DV}$ 

### Refinement Patterns



### Adaptive System



## Outline

- ✓ Introduction
- ✓ Theory and Approach
- ✓ Verification

### Design Examples

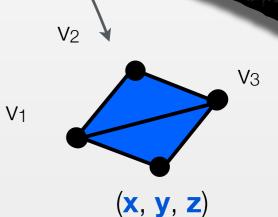
- Implementation
- Sonic boom signature matching
- Adaptive flaps for Truss-braced wing

## Discrete Geometry

- Direct manipulation of surface tessellations
  - CFD-ready always high resolution
  - Allows optimization of "legacy" geometries

### **blender**

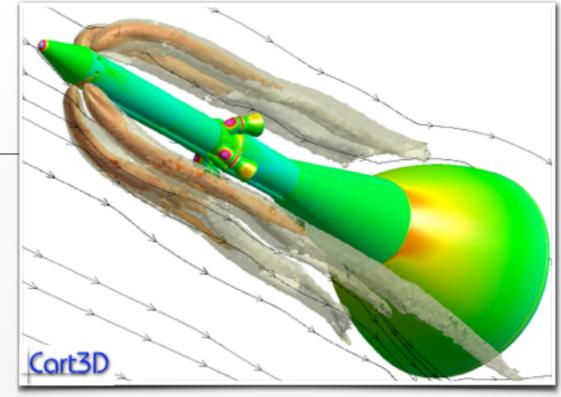
- Serves as **geometry engine** for optimization
- Script-driven surface mesh deformation
- Implemented a number of custom deformation techniques
- (2012) Anderson and Aftosmis, "Parametric Deformation of Discrete Geometry for Aerodynamic Shape Design". AIAA Paper 2012-0965.

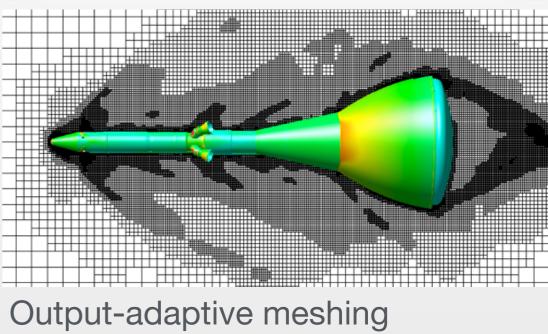


# Cart3D

- Cartesian cut-cell method with automated meshing of complex configurations
- Inviscid solver with adjoint-driven
  - Adaptive meshing
  - Error estimates
  - Functional gradients

Density adjoint of objective







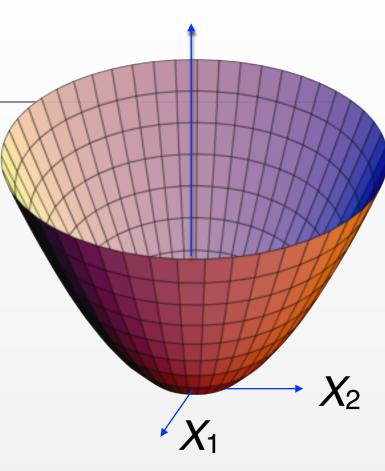
# Optimizer

#### **SNOPT – S**parse Nonlinear **Opt**imizer

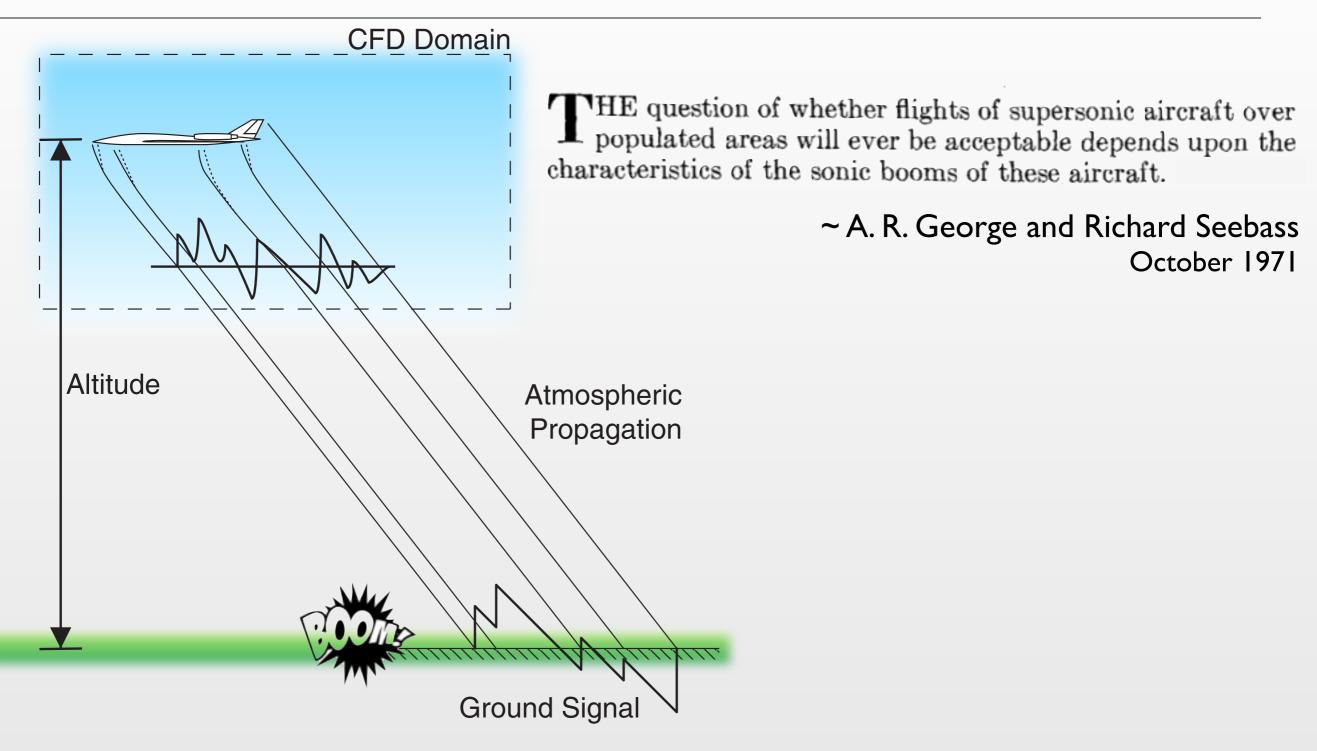
- Quasi-Newton method gradually builds up Hessian approximation
- SQP method handles nonlinear inequality constraints
- Use full-memory BFGS (test cases involve <1000 DVs)</li>

Can also use any general gradient-based optimizer:

► SLSQP, SciPy, Knitro, pyOpt...



### Boom Design

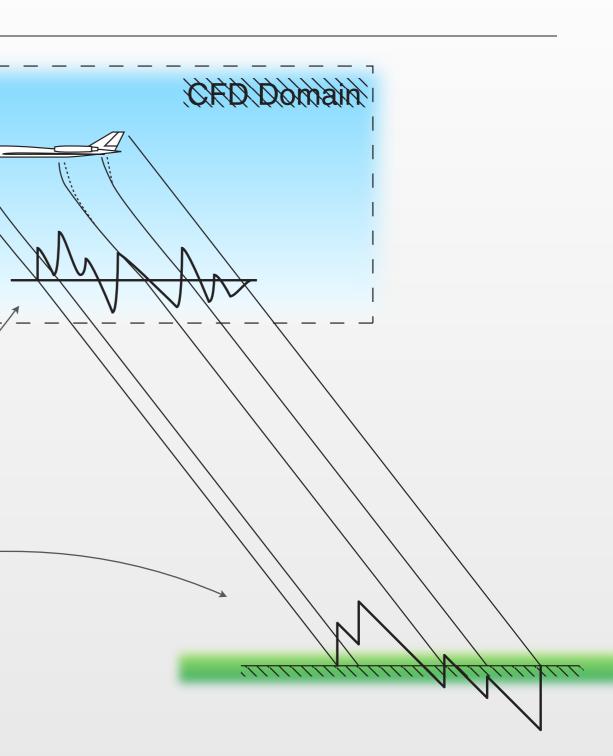


### Inverse Design Procedure

3. **Reshape vehicle** to match the near-field signal

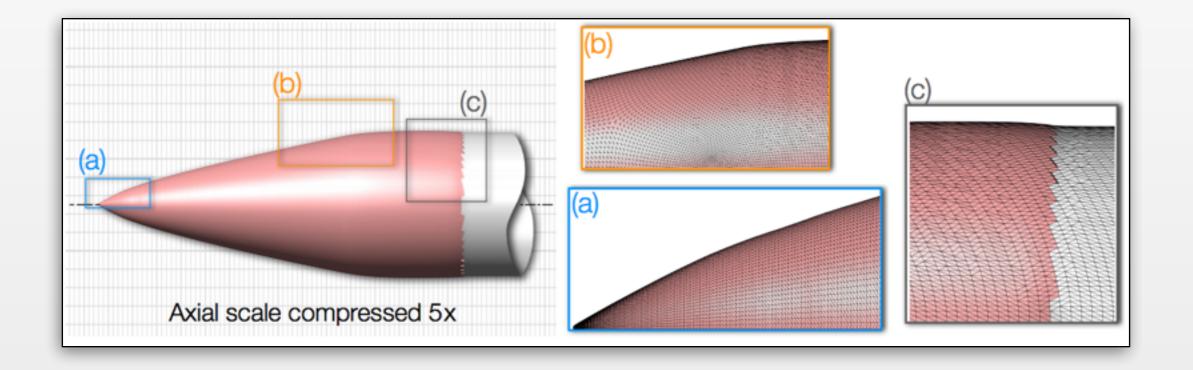
 $\mathcal{J} = \frac{1}{p_{\infty}^2} \int (p - p_{\text{target}})^2 dS$ 

- 2. Find **near-field signal** that meets these requirements
- 1. Determine acceptable noise characteristics at **ground**

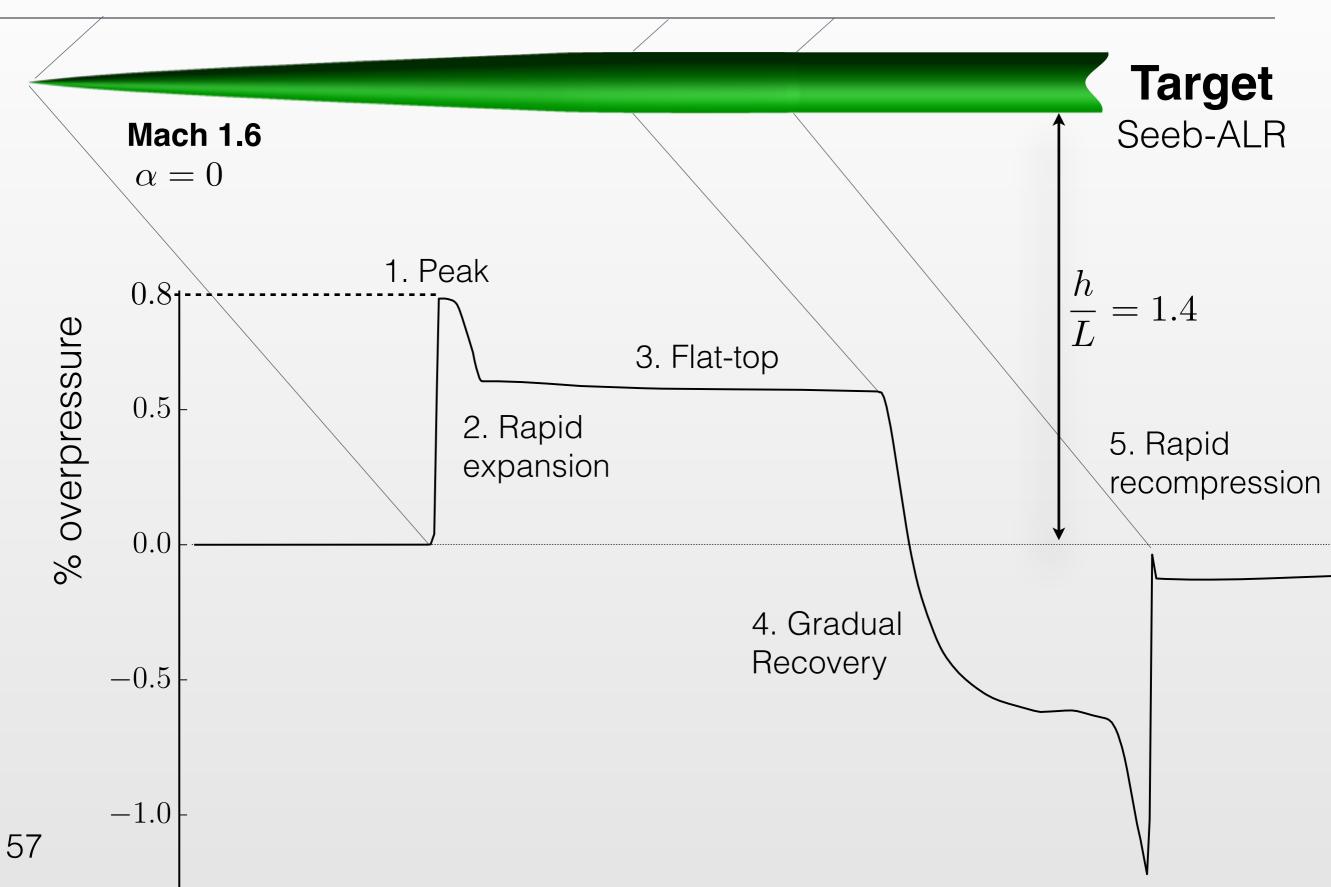




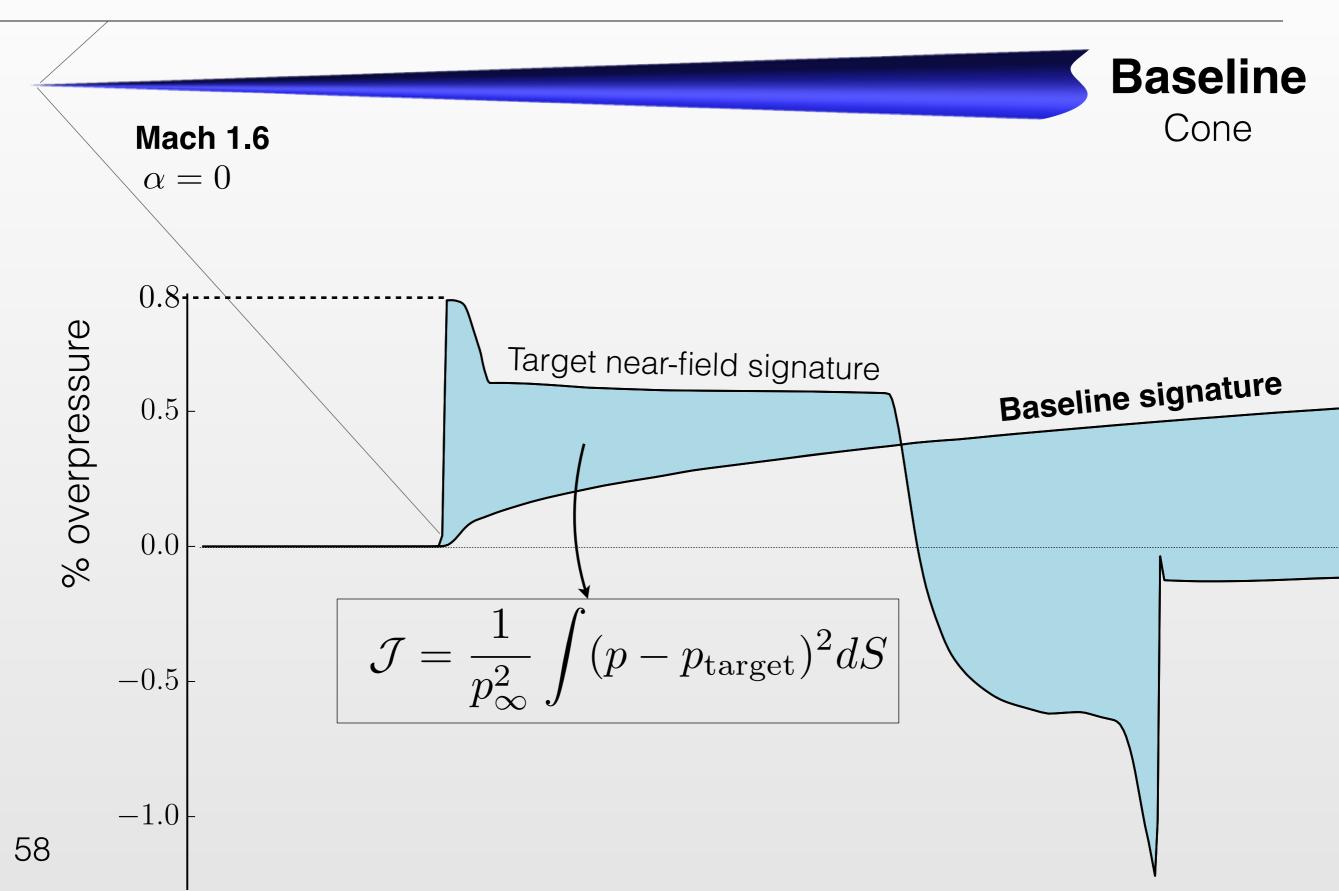
**Target** Seeb-ALR



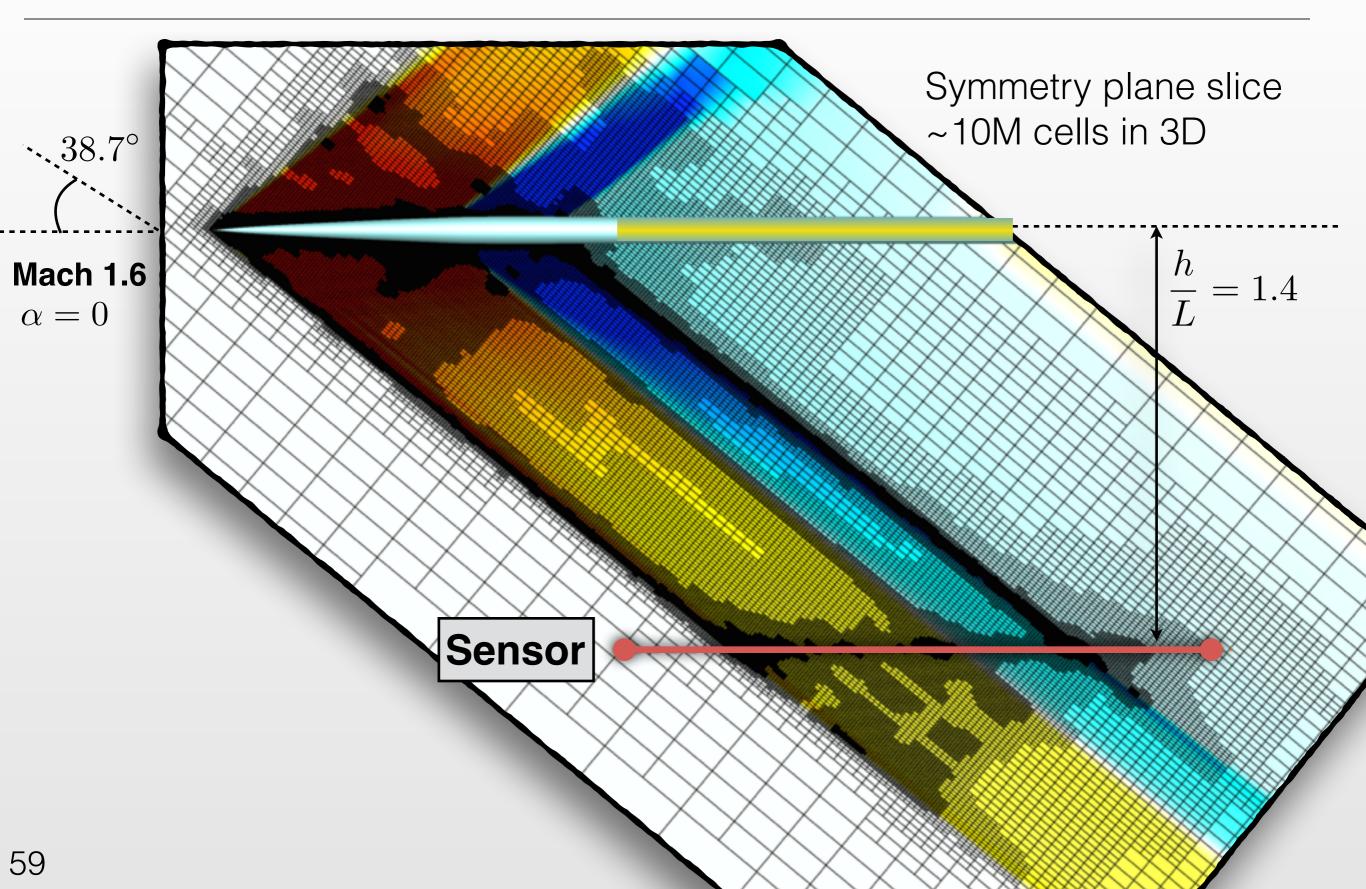
### Target Nearfield Signature



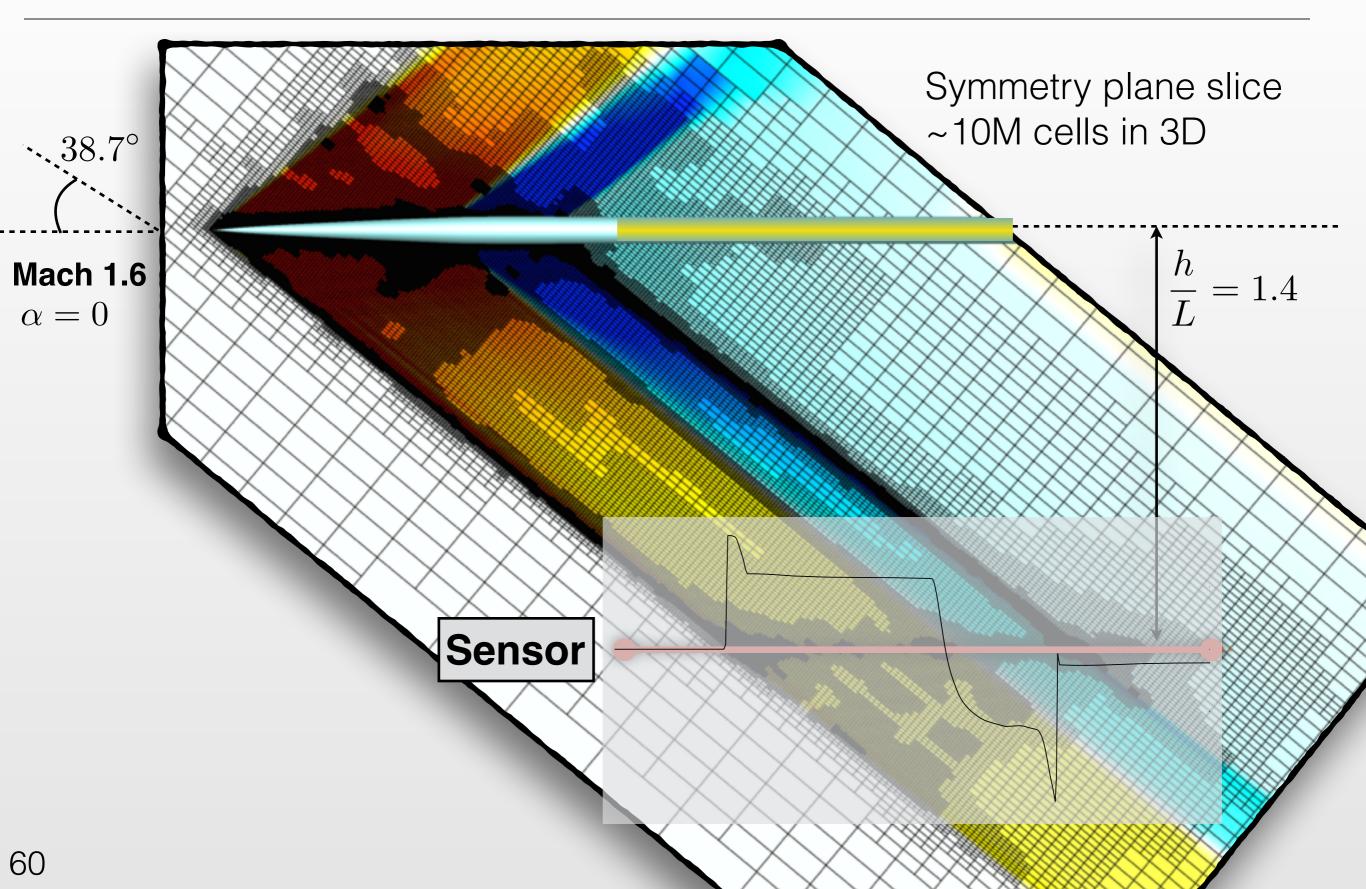
#### **Baseline Geometry**



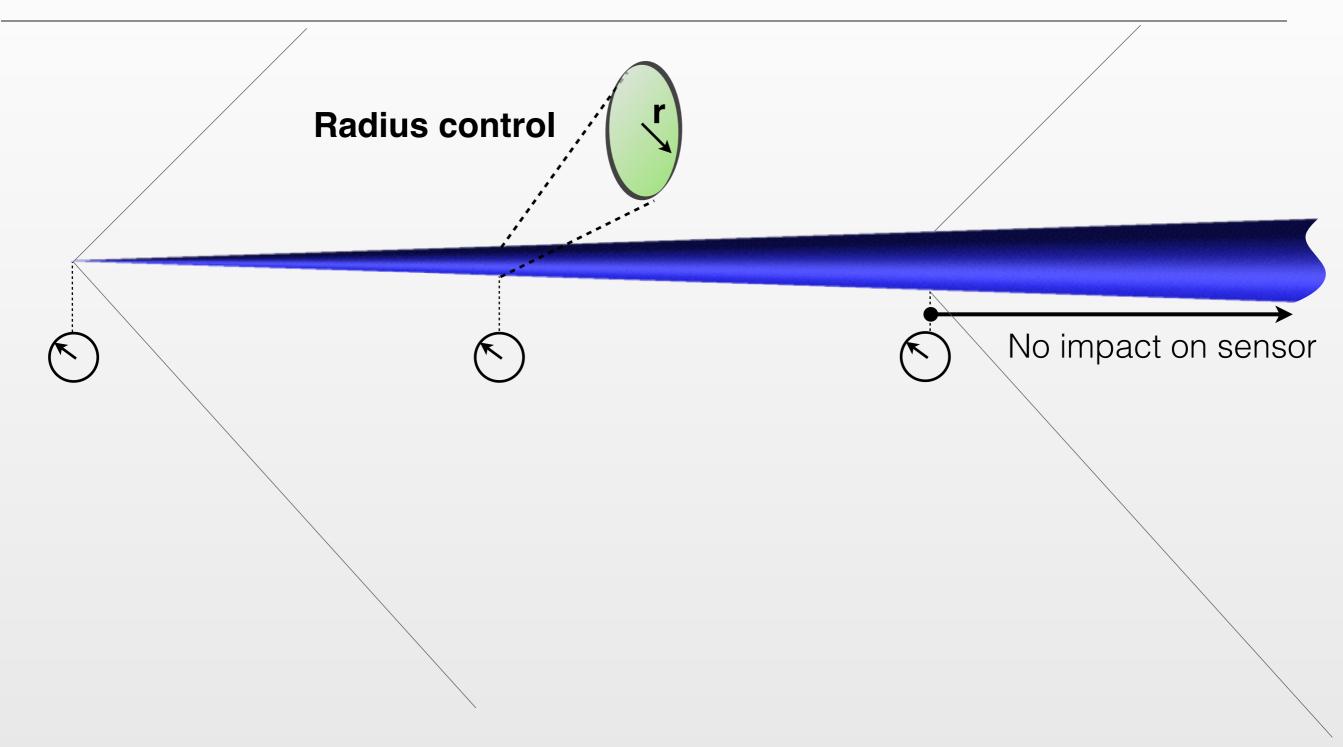
### Mesh Adaptation



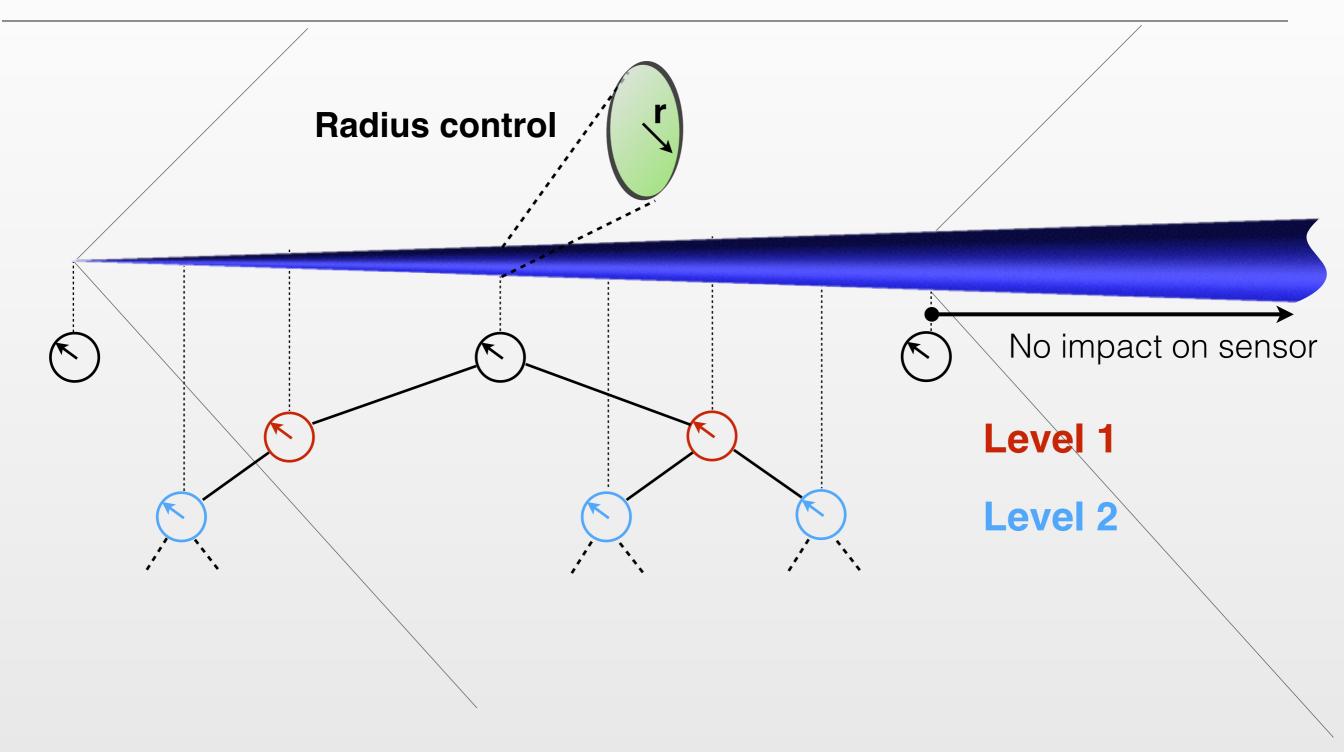
### Mesh Adaptation

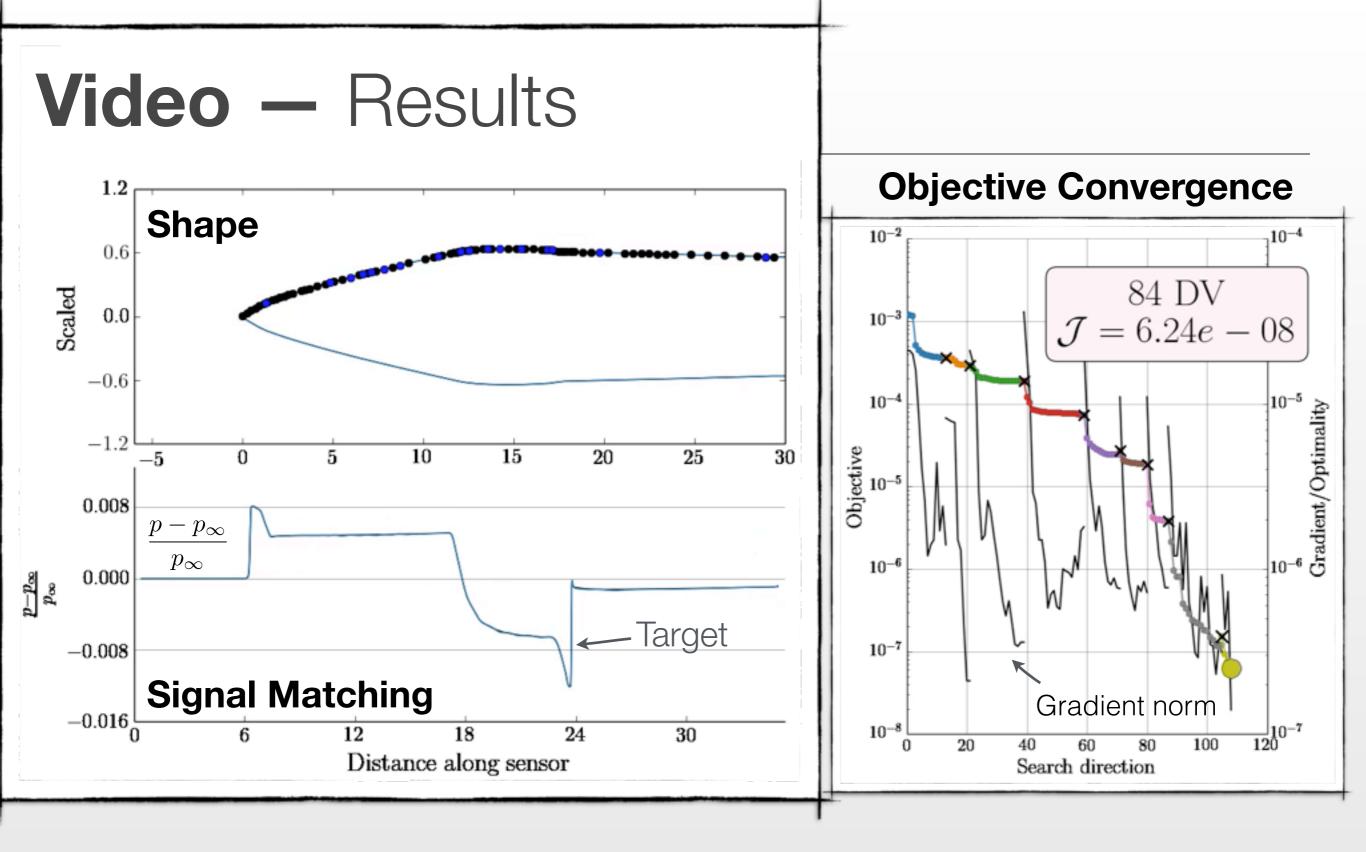


#### Adaptive Parameterization

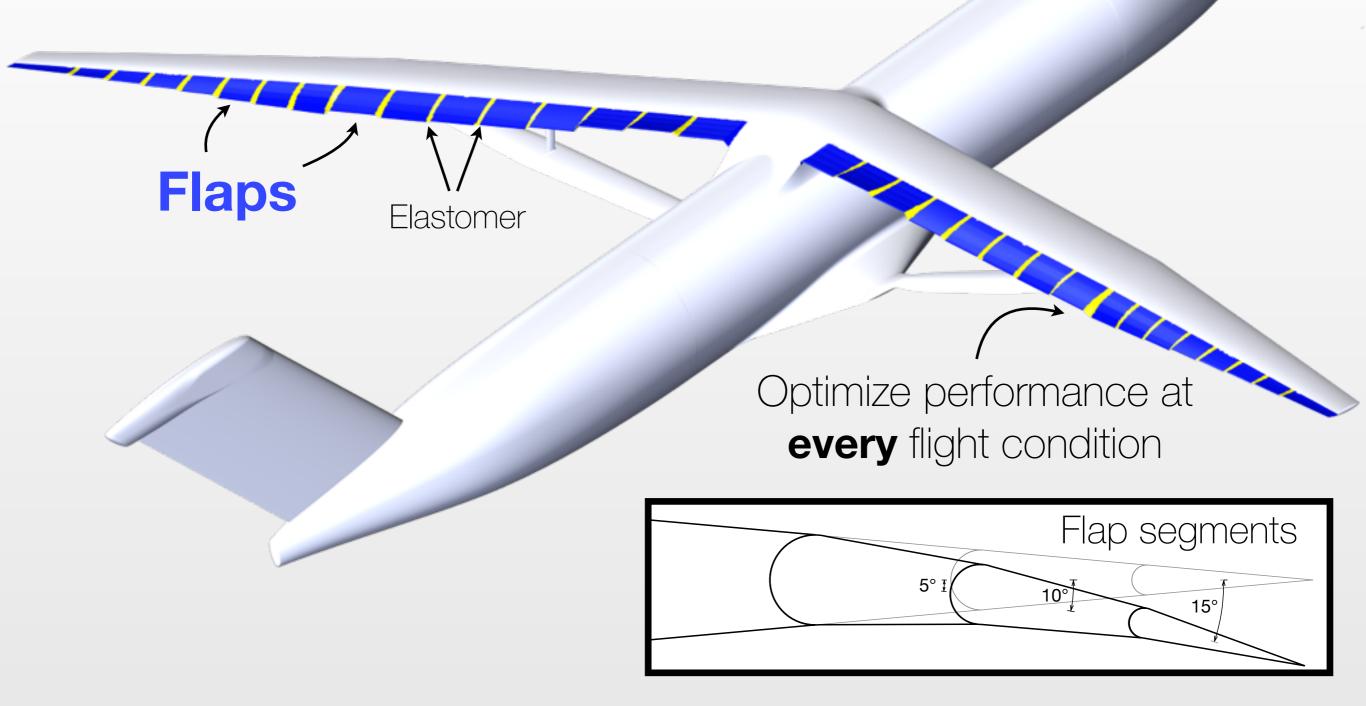


### Adaptive Parameterization

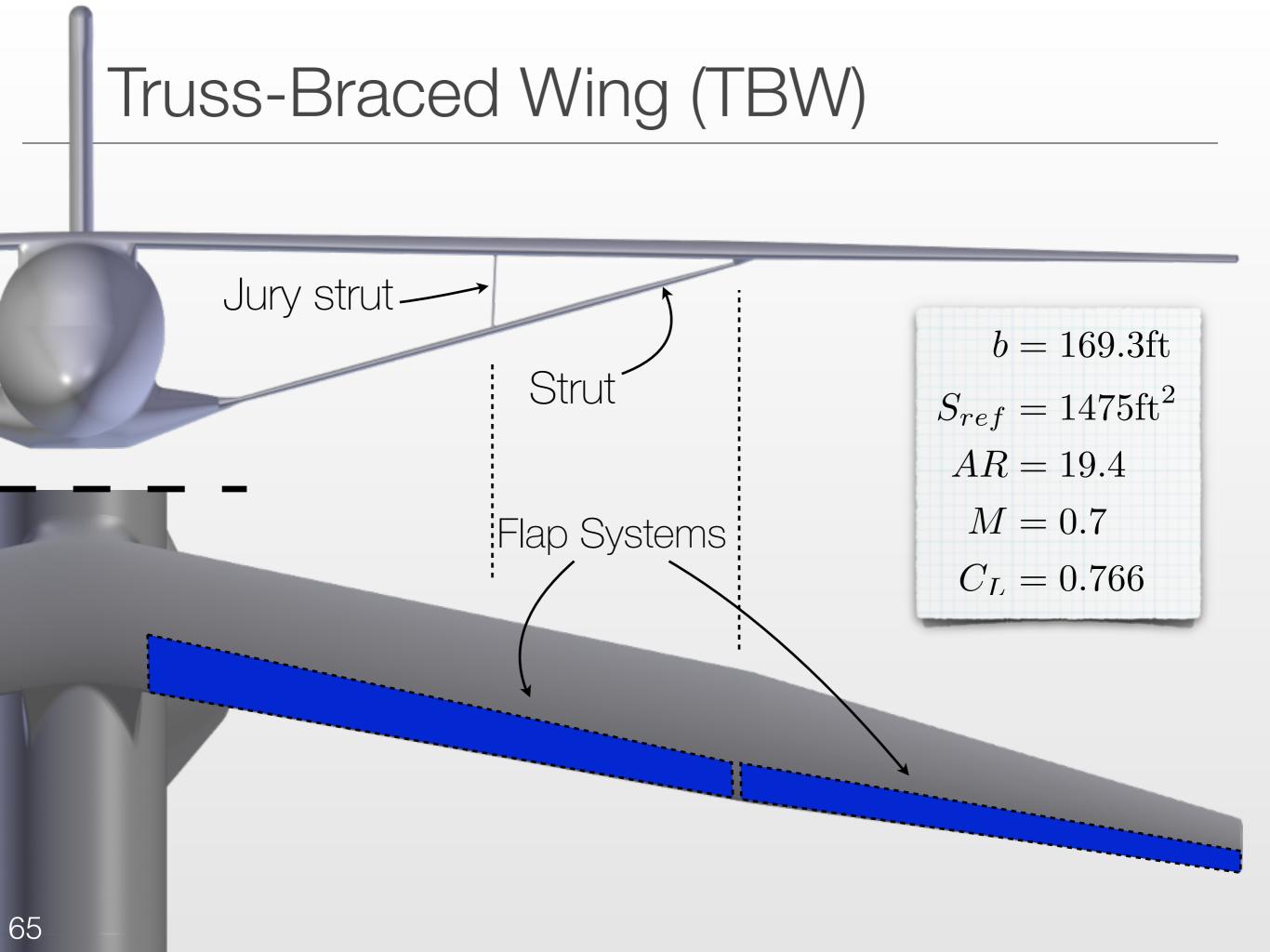




### Adaptive Wing Morphing

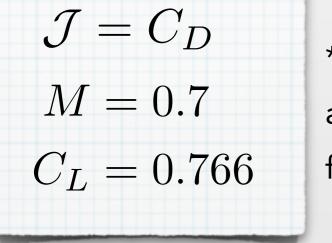


(2015) Rodriguez, Aftosmis, Nemec, Anderson, "Optimized off-design performance of flexible wings with continuous trailing-edge flaps." AIAA Paper 2015–1409, AIAA SciTech 2015, Kissimmee, FL.

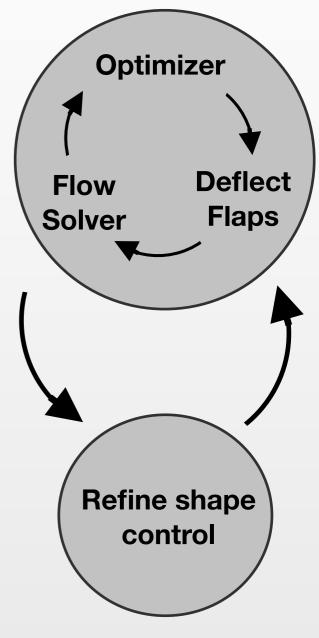


# Flap Adaptation Procedure

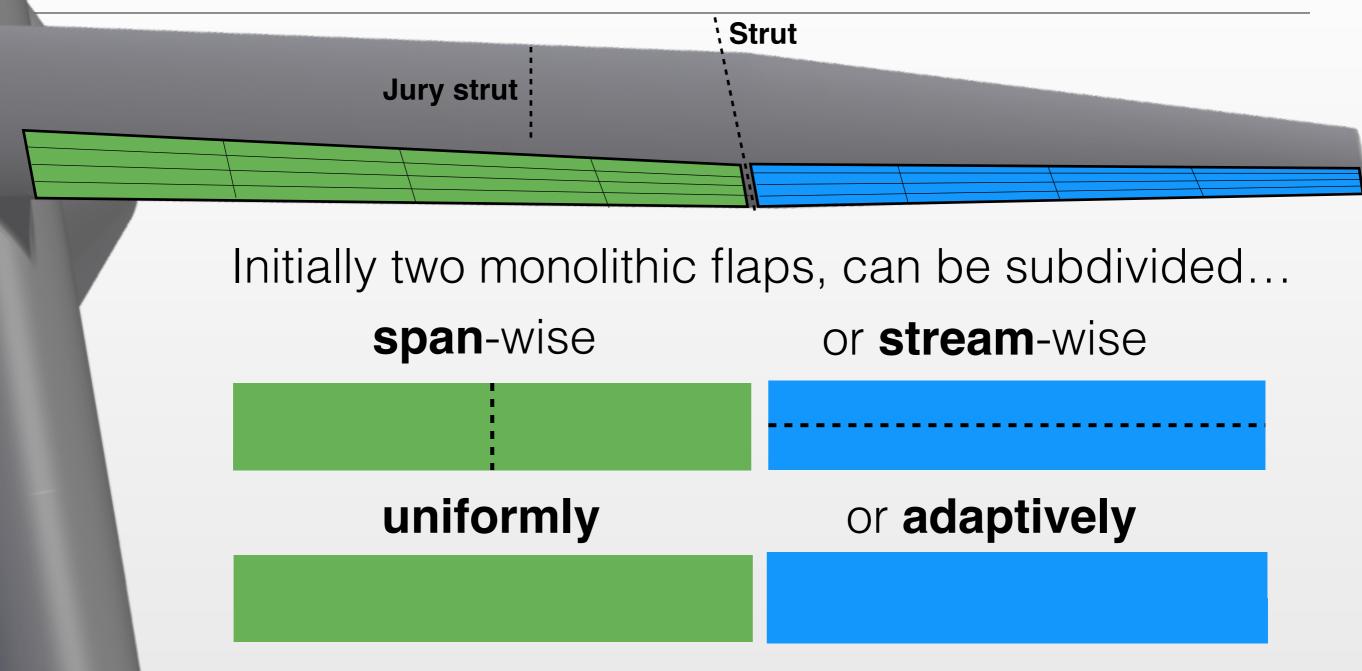
- 1) Morph: Optimize flap deflections for minimum drag.
  - Refine flap topology: Add the one\* additional flap that would best allow the drag to be reduced.



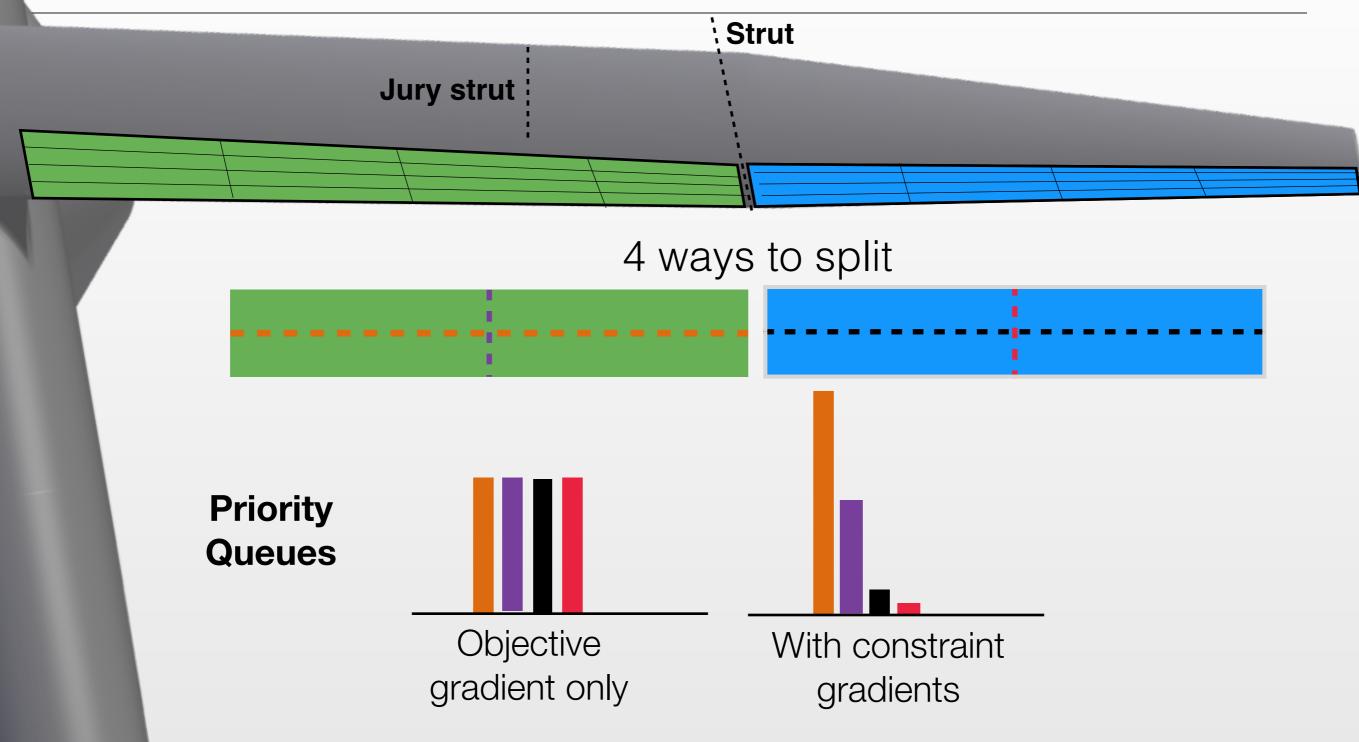
\*Add flaps **one** at a time, because the cost associated with every flap is real — want to find **minimal** parameterization!



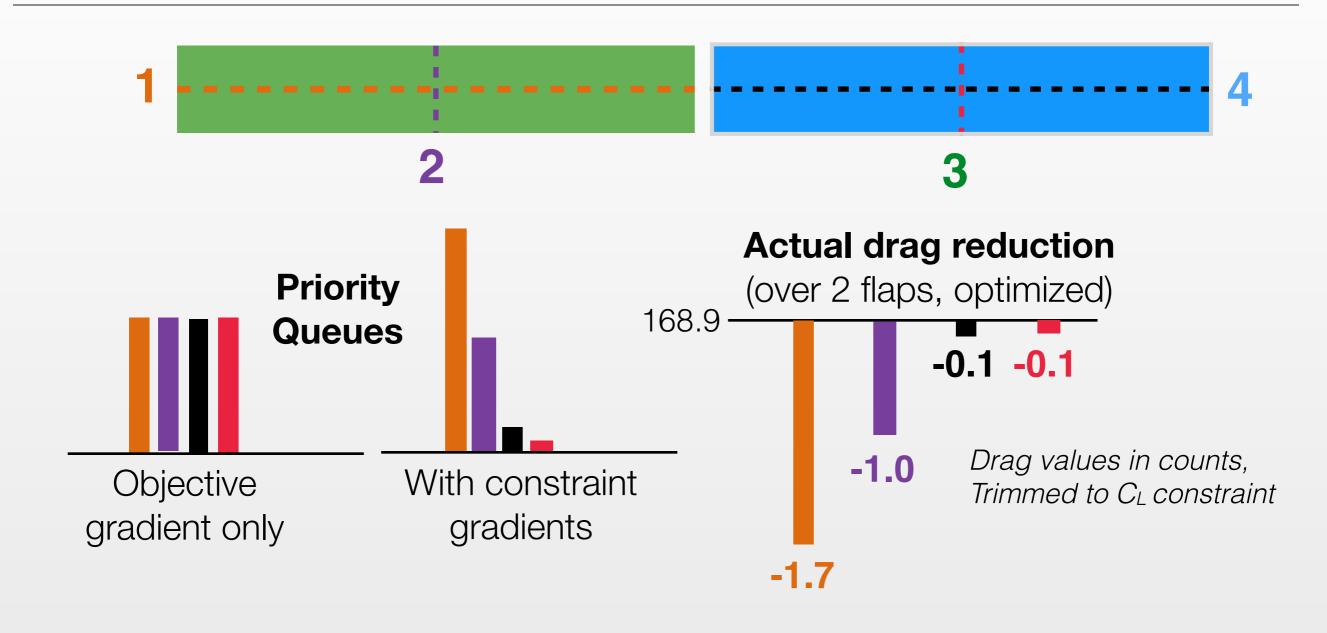
### Flap Refinement



### First Step



## Verification of Ranking



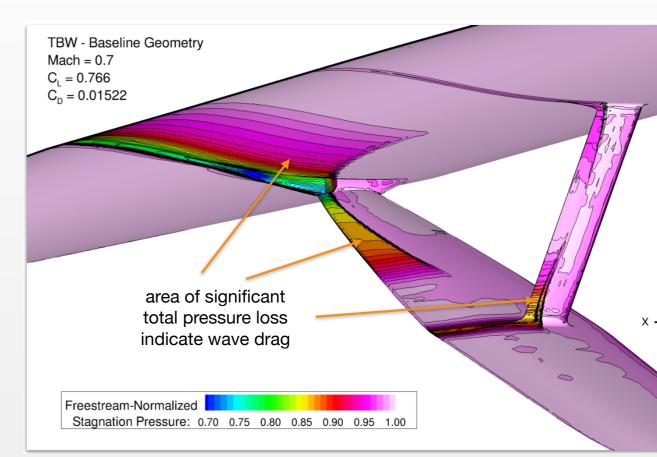
# Flap Deflection History

#### Final flap topology

Inboard	Outboard			
-1.15° <b>-1.65°</b>	-0.6°	-0.4°		
<b>Final deflections</b>				

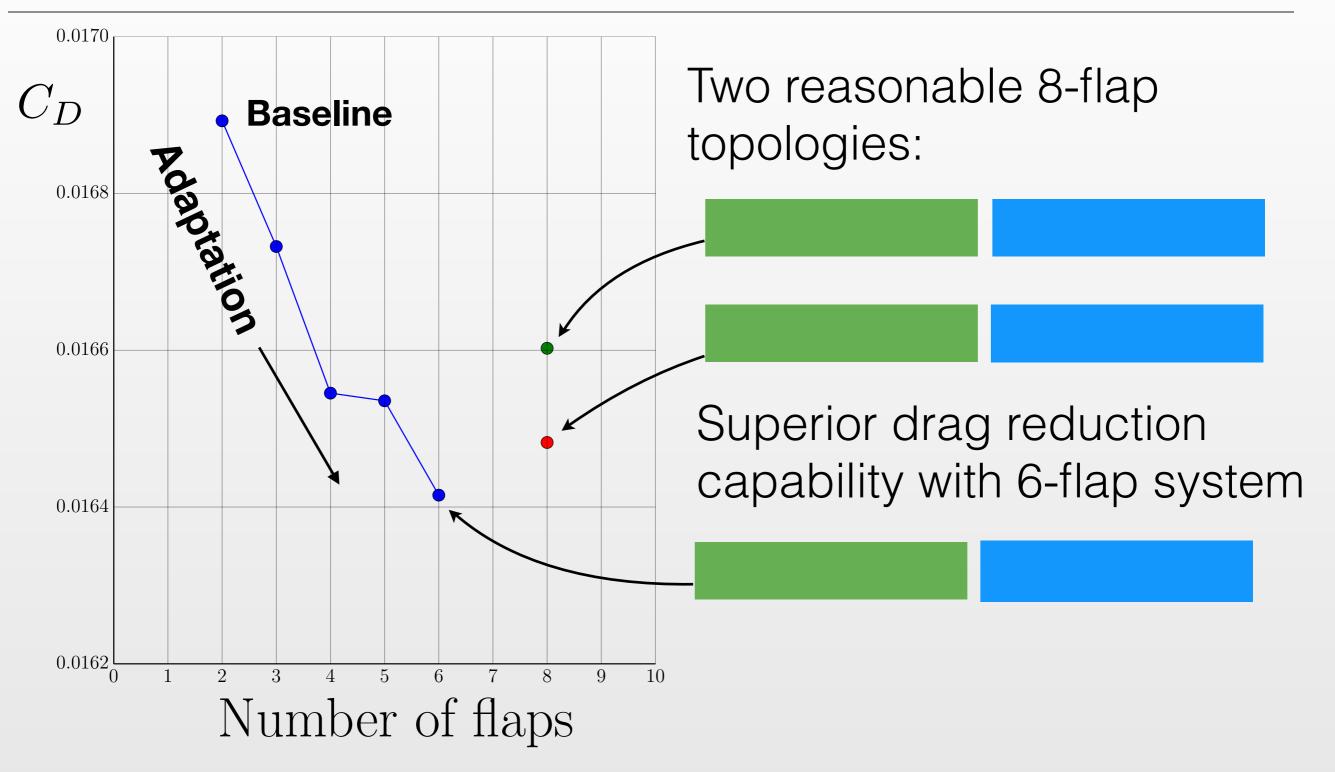
(cumulative deflection at TE)

Negative deflection downward. Alpha lowered to compensate lift.



Baseline geometry has substantial **wave drag** through truss

### Cost vs. Flap Count



71

### Conclusions

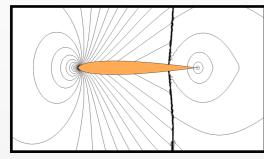
- Demonstrated **adaptive shape parameterization** system for automated, high-fidelity aerodynamic optimization.
  - Enables hands-off design exploration for unfamiliar problems.
  - Provides feedback about the design problem.
- Verification studies confirm that robust **convergence** to continuous optimum is possible.
- A careful adaptive strategy makes the approach substantially **more efficient** both in terms of design variables and computational time.

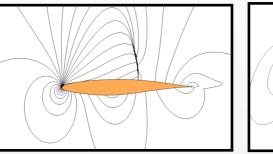
## New Techniques

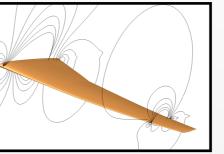
- Goal-oriented **refinement indicator** targeting high potential shape parameters.
  - Substantially improves results over previous best indicator, appropriate for general classes of problems.
  - Leverages information already available during optimization no a priori knowledge required.
- Approximate **Hessian estimation** (prolongation operator)
  - Could also be used to accelerate design in finer design spaces.
- Constructive algorithm to efficiently find an approximate solution to the combinatorial adaptation problem.
- Cost-benefit approaches to automatically determine how many parameters to add and when to trigger refinement.

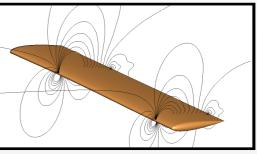
## **Optimization Benchmarks**

Transonic wing and airfoil design benchmarks

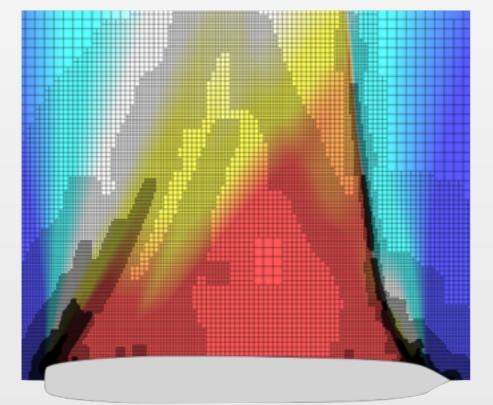


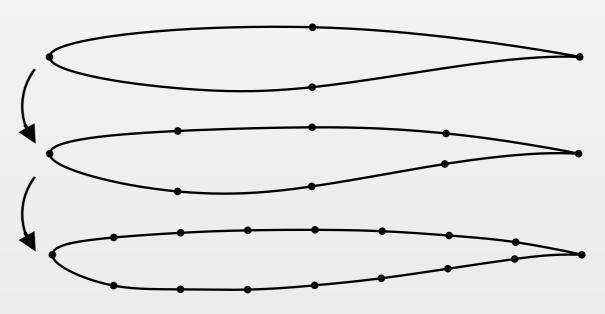






Combined two automated, adaptive elements:





Progressive parameterization

#### Adaptive mesh refinement

<sup>†</sup> (2015) **Anderson**, Nemec, Aftosmis. "Aerodynamic Shape Optimization Benchmarks with Error Control and Automatic Parameterization." AIAA 2015-1719

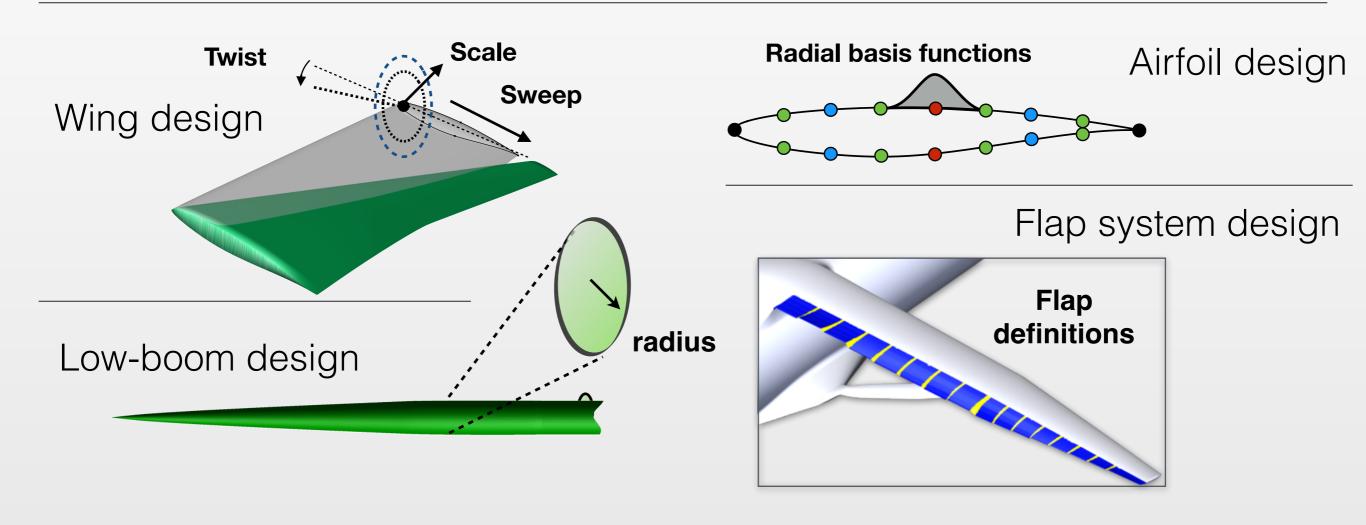
### Publications

- 1. Anderson and Aftosmis, "Parametric Deformation of Discrete Geometry for Aerodynamic Shape Design". AIAA Paper 2012-0965, 50th AIAA ASM Meeting and Exhibit, Nashville, TN, January 2012.
- 2. Anderson, Aftosmis, Nemec, "Constraint-based Shape Parameterization for Aerodynamic Design". ICCFD7 Paper-2001. Seventh International Conference on Computational Fluid Dynamics (ICCFD7), Big Island, HI, July 2012.
- 3. Anderson and Aftosmis, "Adaptive shape parameterization for aerodynamic design." NASA Technical Memorandum, May 2015.
- 4. Rodriguez, Aftosmis, Nemec, Anderson, "Optimized off-design performance of flexible wings with continuous trailing-edge flaps." AIAA Paper 2015–1409, AIAA SciTech 2015, Kissimmee, FL, http://dx.doi.org/10.2514/6.2014-1409, January 2015.
- 5. Anderson, Nemec, Aftosmis, "Aerodynamic shape optimization benchmarks with error control and automatic parameterization." AIAA Paper 2015-1719, Kissimmee, FL, http://dx.doi.org/ 10.2514/6.2015-1719, January 2015.
- 6. Anderson and Aftosmis, "Adaptive shape control for aerodynamic design." AIAA Paper 2015-0398, AIAA SciTech 2015, Kissimmee, FL, http://dx.doi.org/10.2514/6.2015-0398, January 2015.

## Future Work

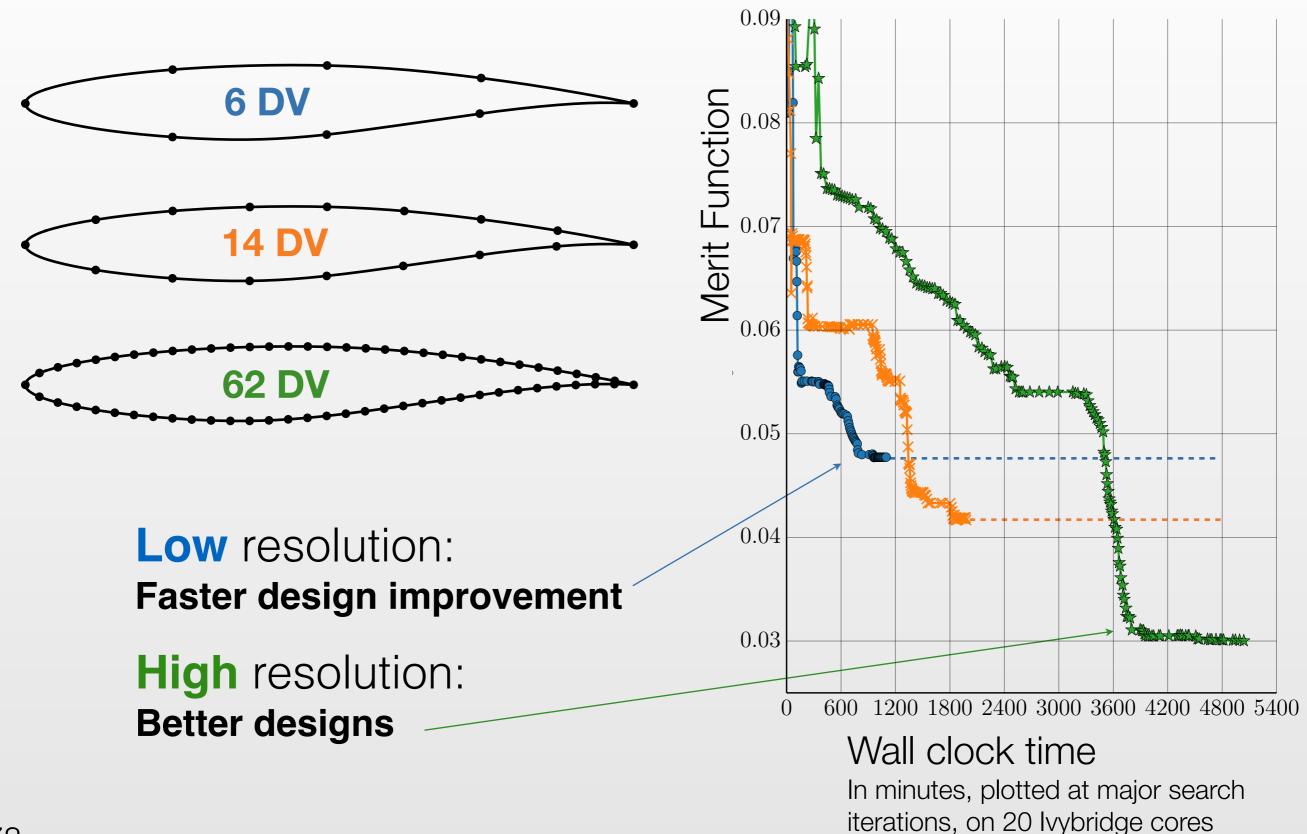
Major outstanding topic:

Discovering effective classes of shape control

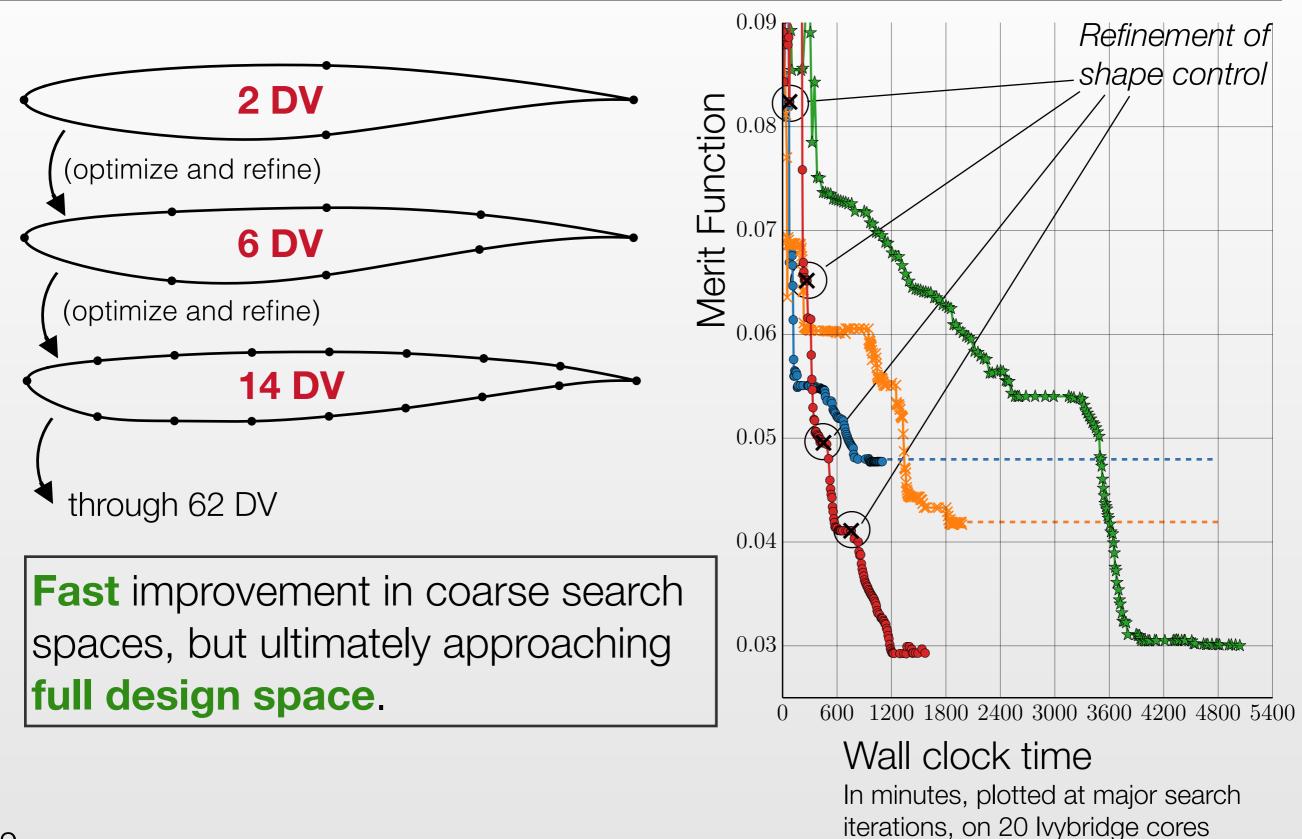


# Backup Slides

#### But How Fast Is It?



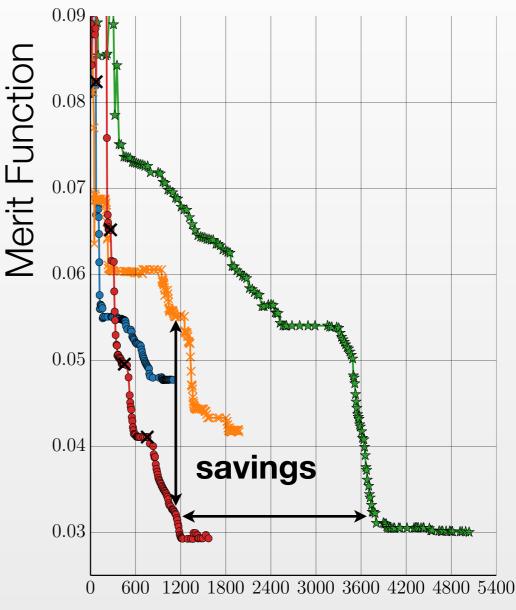
#### Progressive vs. Static



## Cost

#### Factors contributing to acceleration:

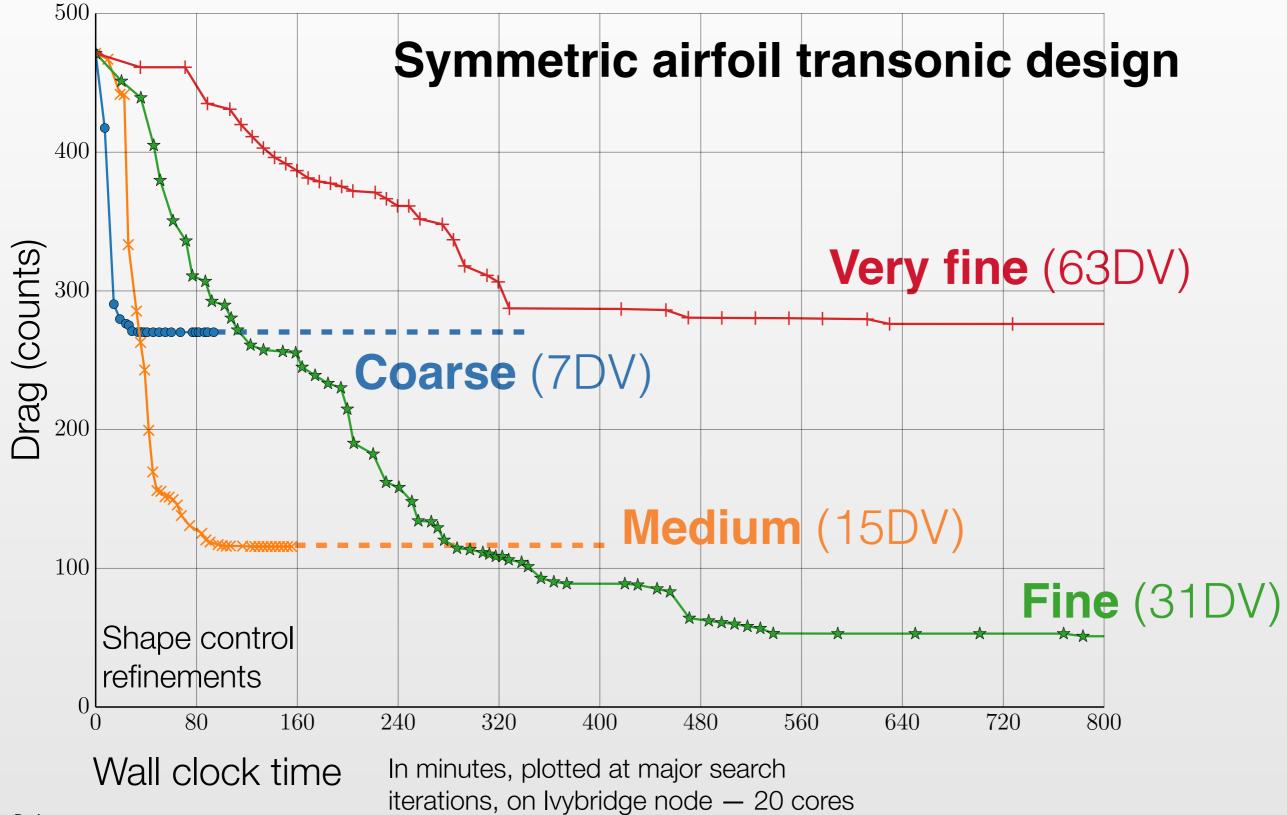
- Early on there are few design variables:
  - Accelerates **BFGS rate of improvement** w.r.t search direction.
  - Reduces # of shape sensitivities and gradient projections.
- Later, more design variables are added, preventing optimization from stalling.



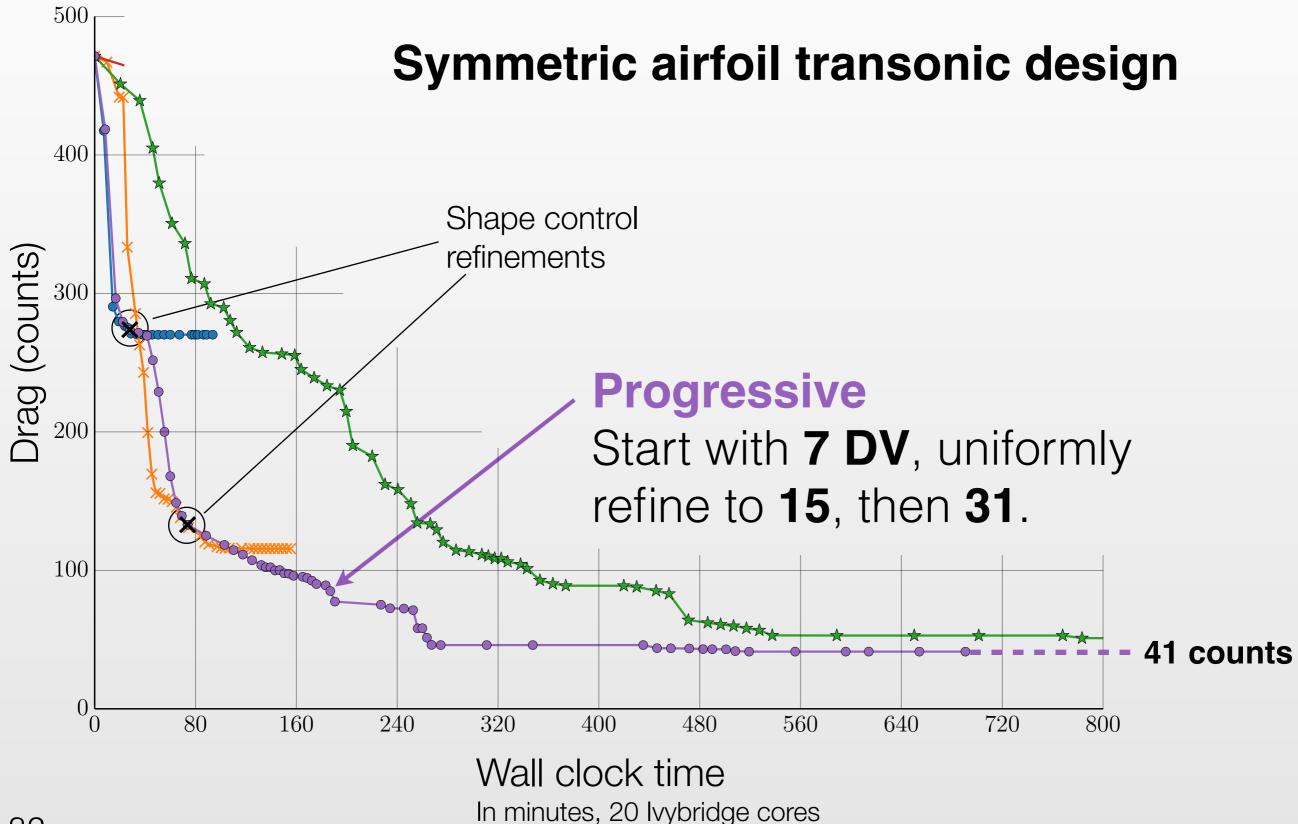
#### Wall clock time

In minutes, plotted at major search iterations, on 20 lvybridge cores

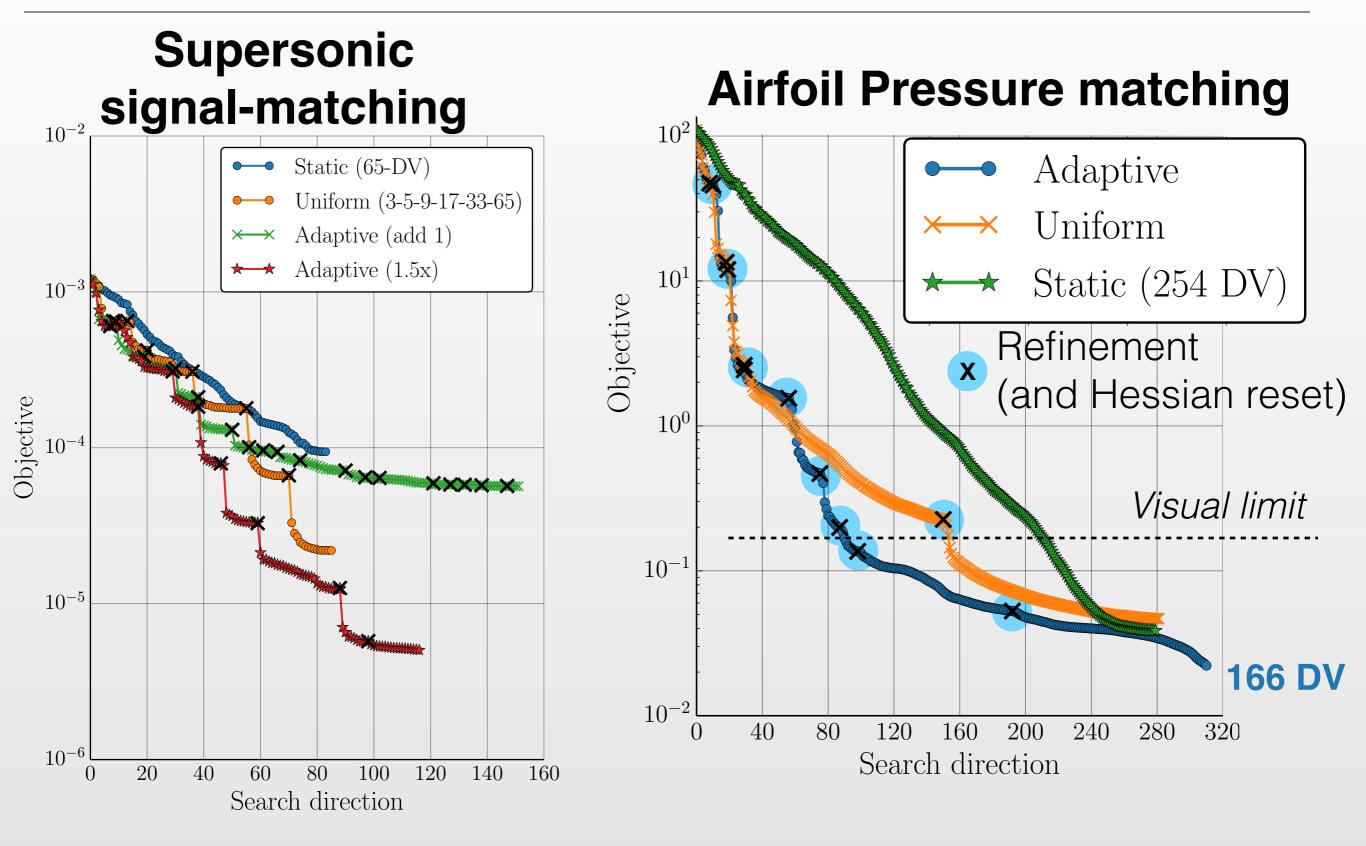
## Impact of Parameterization



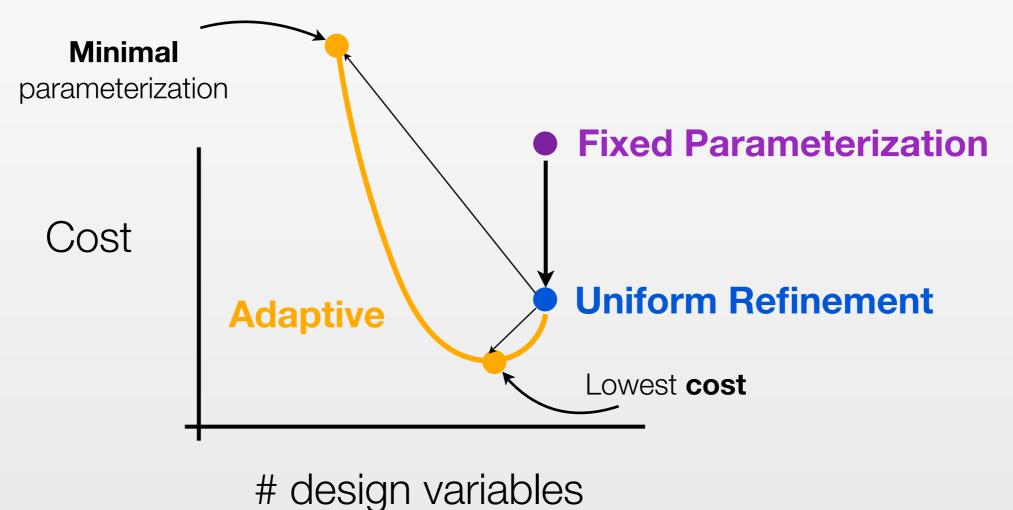
### Progressive vs. Static



## Adaptive vs. Uniform



#### Goals of Adaptation



to solve problem